

ヒッグス物理で迫るCPの破れの起源

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Collaboration with

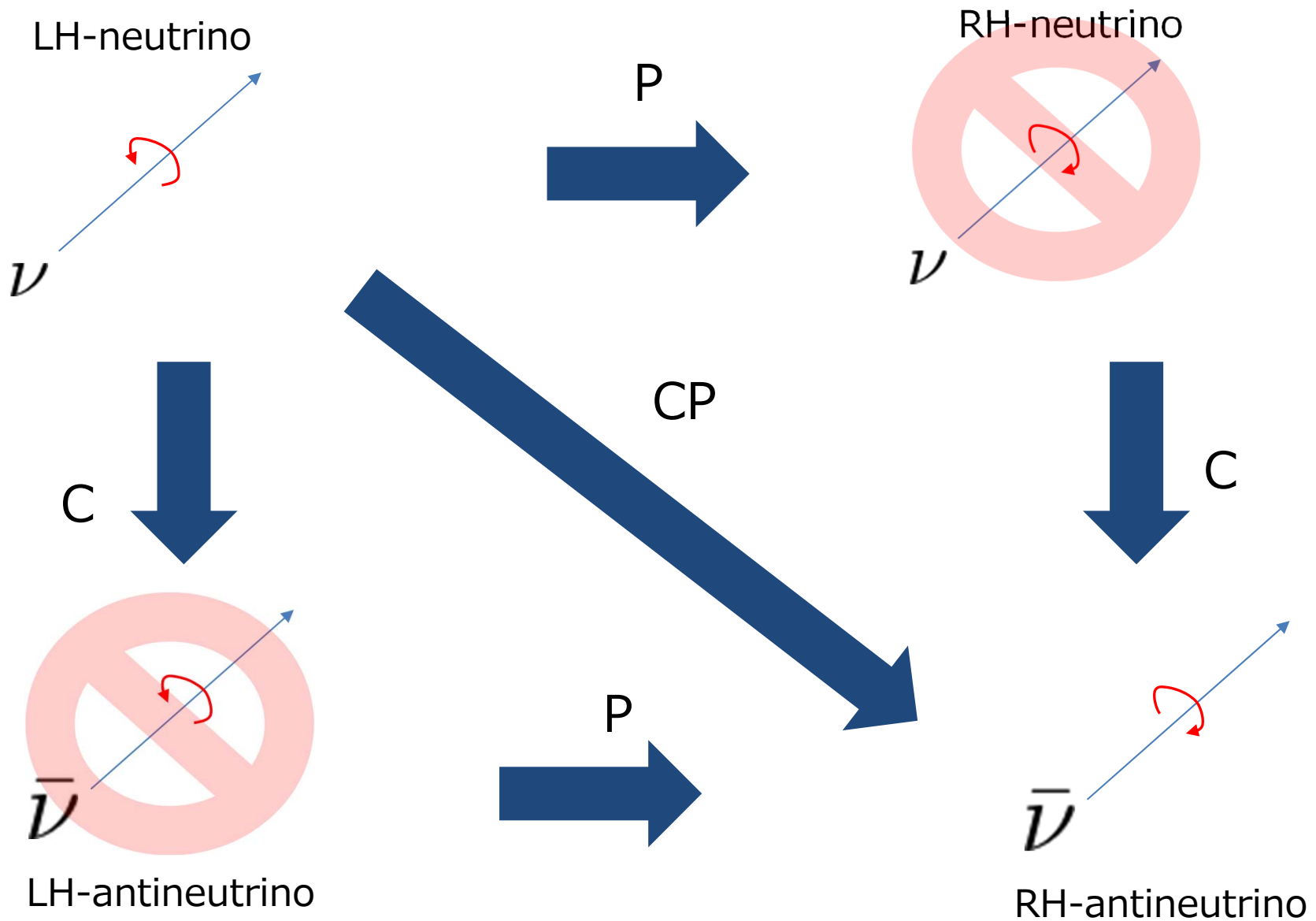
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2505.05104 (hep-ph)

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CP-transformation



CP-violation

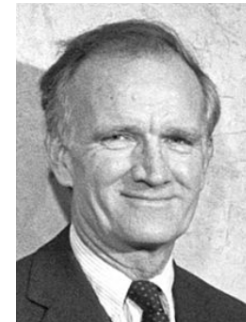
- CP-violation has been discovered by Kaon decays in 1964.

$$K_L \rightarrow \pi\pi\pi \quad \text{CP-odd}$$

$$K_L \rightarrow \pi\pi \quad \text{CP-even}$$



Cronin



Fitch

- In the SM, CPV can be explained by the Kobayashi-Maskawa phase (1973).

$$V_{\text{CKM}} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{bmatrix} \begin{bmatrix} c_{13} & 0 & s_{13}e^{-i\delta_{13}} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta_{13}} & 0 & c_{13} \end{bmatrix} \begin{bmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

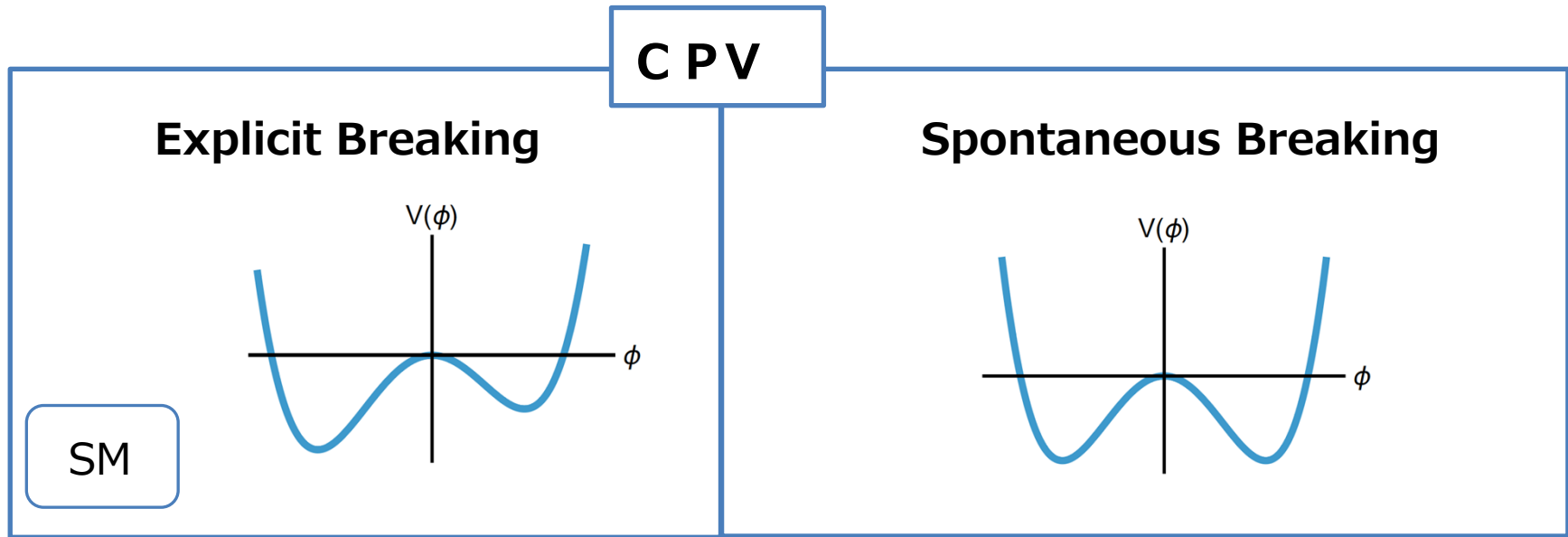


Kobayashi

Maskawa

Question: What is the origin of the KM phase?

Origin of CP-violation



Let us consider 2HDMs as a simple example of SCPV.

SCPV 2HDM: T. D. Lee (1973)

SCPV {
Inevitable non-decoupling Higgs sectors
Flavor misalignment



A Theory of Spontaneous T Violation

T.D. Lee (Columbia U.)

1973

Citations per year



SCPV in 2HDMs

□ VEVs $\langle \Phi_1 \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v_1 \end{pmatrix}, \quad \langle \Phi_2 \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v_2 e^{i\xi} \end{pmatrix}$

□ Potential $V = \mu_1^2 |\Phi_1|^2 + \mu_2^2 |\Phi_2|^2 - (\mu_3^2 \Phi_1^\dagger \Phi_2 + \text{h.c.})$ $\mu_i^2, \lambda_j \in \mathbb{R}$

$$+ \frac{\lambda_1}{2} |\Phi_1|^4 + \frac{\lambda_2}{2} |\Phi_2|^4 + \lambda_3 |\Phi_1|^2 |\Phi_2|^2 + \lambda_4 |\Phi_1^\dagger \Phi_2|^2$$

$$+ \frac{\lambda_5}{2} (\Phi_1^\dagger \Phi_2)^2 + \lambda_6 |\Phi_1|^2 (\Phi_1^\dagger \Phi_2) + \lambda_7 |\Phi_2|^2 (\Phi_1^\dagger \Phi_2) + \text{h.c.}$$

$\xrightarrow{\text{VEV}} v_1 v_2 \left(-\mu_3^2 \cos \xi + \frac{\lambda_5}{4} v_1 v_2 \cos 2\xi + \frac{\lambda_6}{2} v_1^3 v_2 \cos \xi + \frac{\lambda_7}{2} v_1 v_2^3 \cos \xi \right) + \xi \text{ independent terms}$

$\frac{\partial V}{\partial \xi} \rightarrow v_1 v_2 \sin \xi \left(\mu_3^2 - \lambda_5 v_1 v_2 \cos \xi - \frac{\lambda_6}{2} v_1^3 v_2 - \frac{\lambda_7}{2} v_1 v_2^3 \right)$

$\frac{\partial V}{\partial \xi} = 0$



$$\mu_3^2 = v_1 v_2 \left(\lambda_5 \cos \xi + \frac{\lambda_6}{2} v_1^2 + \frac{\lambda_7}{2} v_2^2 \right), \quad \xi \neq n\pi$$

Condition for SCPV

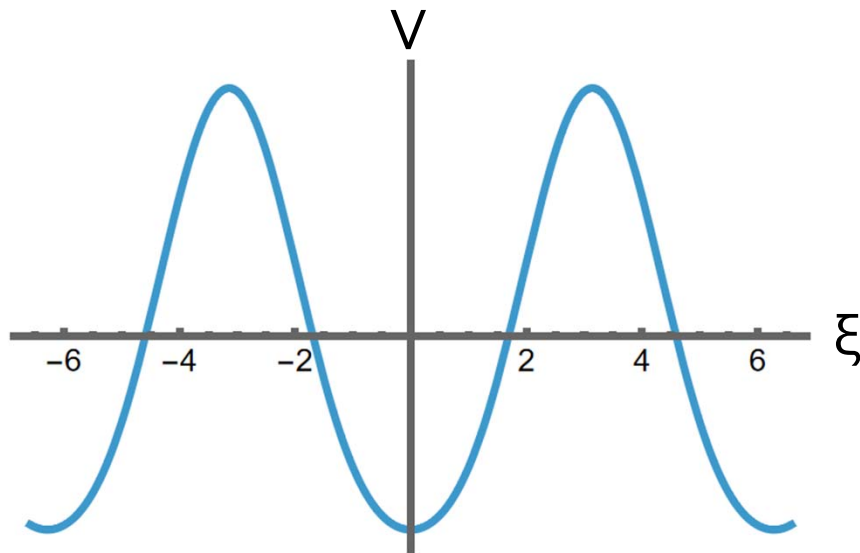
Vacuum Structure (Soft Z_2 case: $\lambda_6 = \lambda_7 = 0$)

$$V_{\text{vac}} = v_1 v_2 \left(-\mu_3^2 \cos \xi + \frac{\lambda_5}{4} v_1 v_2 \cos 2\xi \right) + \text{const.}$$

$$\frac{\partial V_{\text{vac}}}{\partial \xi} = v_1 v_2 \sin \xi (\mu_3^2 - \lambda_5 v_1 v_2 \cos \xi)$$

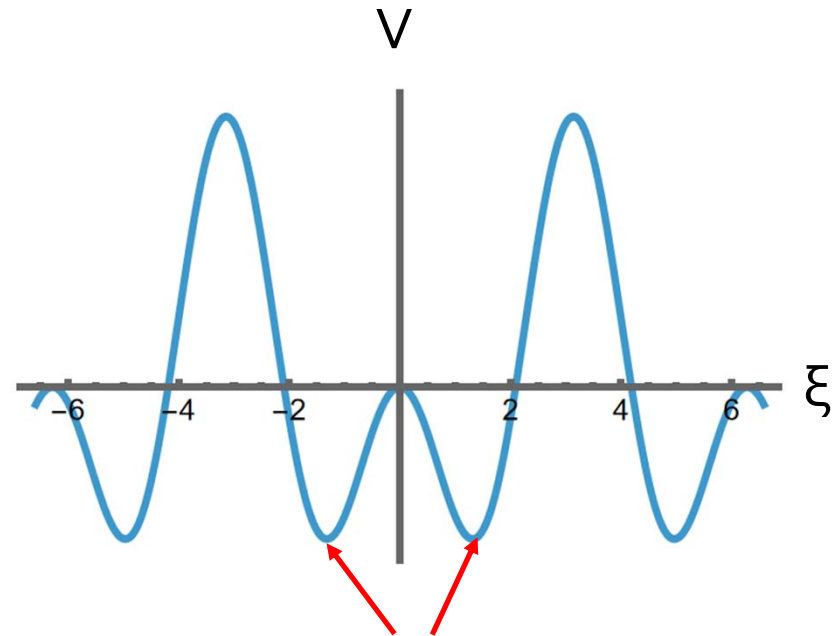
Vac. condition for SCPV: $\cos \xi = \frac{\mu_3^2}{v_1 v_2 \lambda_5}$

$$\mu_3^2 > v_1 v_2 \lambda_5$$



No CPV

$$\mu_3^2 < v_1 v_2 \lambda_5$$



Degenerate CPV vacua $\rightarrow$ SCPV

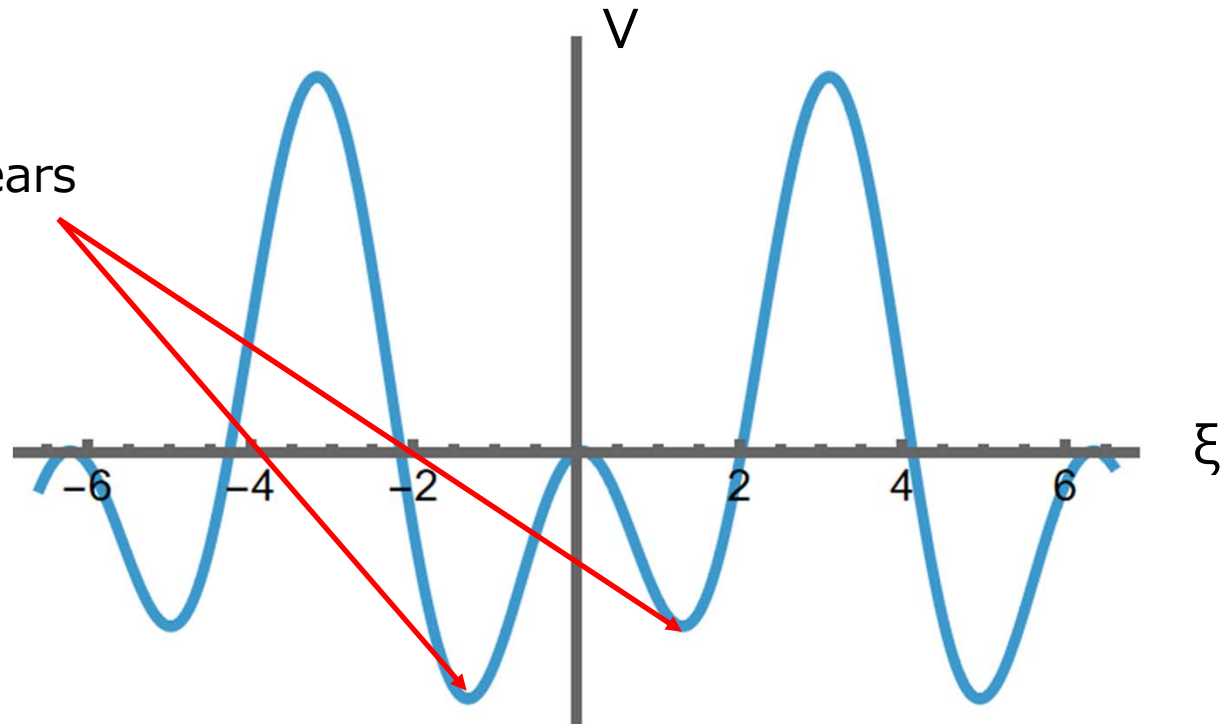
Vacuum Structure (Soft Z_2 case: $\lambda_6 = \lambda_7=0$)

If we introduce an explicit CPV term e.g, $\text{Im}[\mu_3^2] \neq 0$, potential becomes

$$V_{\text{vac}} = v_1 v_2 \left(-\mu_3^2 \cos \xi + \frac{\lambda_5}{4} v_1 v_2 \cos 2\xi + \text{Im}[\mu_3^2] \sin \xi \right) + \text{const.}$$

Degeneracy disappears

→ Explicit CPV



We focus on SCPV 2HDM.

Potential

□ Most general form with CP-invariance

$$\begin{aligned}
 V = & \mu_1^2 |\Phi_1|^2 + \mu_2^2 |\Phi_2|^2 - (\mu_3^2 \Phi_1^\dagger \Phi_2 + \text{h.c.}) \\
 & + \frac{\lambda_1}{2} |\Phi_1|^4 + \frac{\lambda_2}{2} |\Phi_2|^4 + \lambda_3 |\Phi_1|^2 |\Phi_2|^2 + \lambda_4 |\Phi_1^\dagger \Phi_2|^2 \\
 & + \frac{\lambda_5}{2} (\Phi_1^\dagger \Phi_2)^2 + \lambda_6 |\Phi_1|^2 (\Phi_1^\dagger \Phi_2) + \lambda_7 |\Phi_2|^2 (\Phi_1^\dagger \Phi_2) + \text{h.c.}
 \end{aligned}
 \quad \mu_i^2, \lambda_j \in \mathbb{R}$$

□ Higgs fields

$$\begin{pmatrix} \Phi_1 \\ \Phi_2 \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ 0 & e^{i\xi} \end{pmatrix} \begin{pmatrix} \cos \beta & -\sin \beta \\ \sin \beta & \cos \beta \end{pmatrix} \begin{pmatrix} \Phi \\ \Phi' \end{pmatrix}$$

NGBs

$$\Phi = \begin{bmatrix} G^+ \\ \frac{1}{\sqrt{2}}(h'_1 + v + iG^0) \end{bmatrix}$$

Charged Higgs

$$\Phi' = \begin{bmatrix} H^+ \\ \frac{1}{\sqrt{2}}(h'_2 + ih'_3) \end{bmatrix}$$

□ Vacuum conditions

$$\mu_1^2 = -\frac{v^2}{2}(\lambda_1 c_\beta^2 + \lambda_3 s_\beta^2 - \lambda_4 s_\beta^2 - \lambda_5 s_\beta^2 + \lambda_6 s_{2\beta} c_\xi),$$

$$\mu_2^2 = -\frac{v^2}{2}(\lambda_2 s_\beta^2 + \lambda_3 c_\beta^2 + \lambda_4 c_\beta^2 - \lambda_5 c_\beta^2 + \lambda_7 s_{2\beta} c_\xi),$$

$$\mu_3^2 = \frac{v^2}{2}(\lambda_5 s_{2\beta} c_\xi + \lambda_6 c_\beta^2 + \lambda_7 s_\beta^2).$$

Neutral Higgses

Mass formulae

□ Charged-Higgs mass

$$m_{H^\pm}^2 = \frac{v^2}{2}(\lambda_5 - \lambda_4)$$

$$\begin{pmatrix} h'_1 \\ h'_2 \\ h'_3 \end{pmatrix} = R_{23}(\alpha_{23})R_{13}(\alpha_{13})R_{12}(\alpha_{12}) \begin{pmatrix} H_1 \\ H_2 \\ H_3 \end{pmatrix}$$

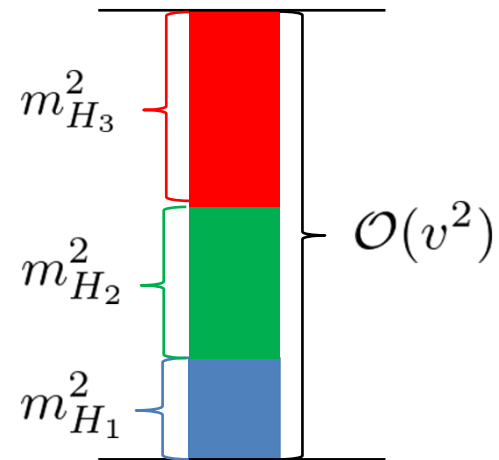
□ Neutral Higgs masses (3×3 mass matrix)

$$\text{tr}[\mathcal{M}] = \sum_{i=1,3} m_{H_i}^2 = v^2[\lambda_1 c_\beta^2 + \lambda_2 s_\beta^2 + \lambda_5 + (\lambda_6 + \lambda_7)s_{2\beta}c_\xi]$$

➡ No decoupling limit

$$\text{Det}[\mathcal{M}] = \prod_{i=1,3} m_{H_i}^2 \propto \frac{v^6 s_\xi^2}{(t_\beta + 1/t_\beta)^2}$$

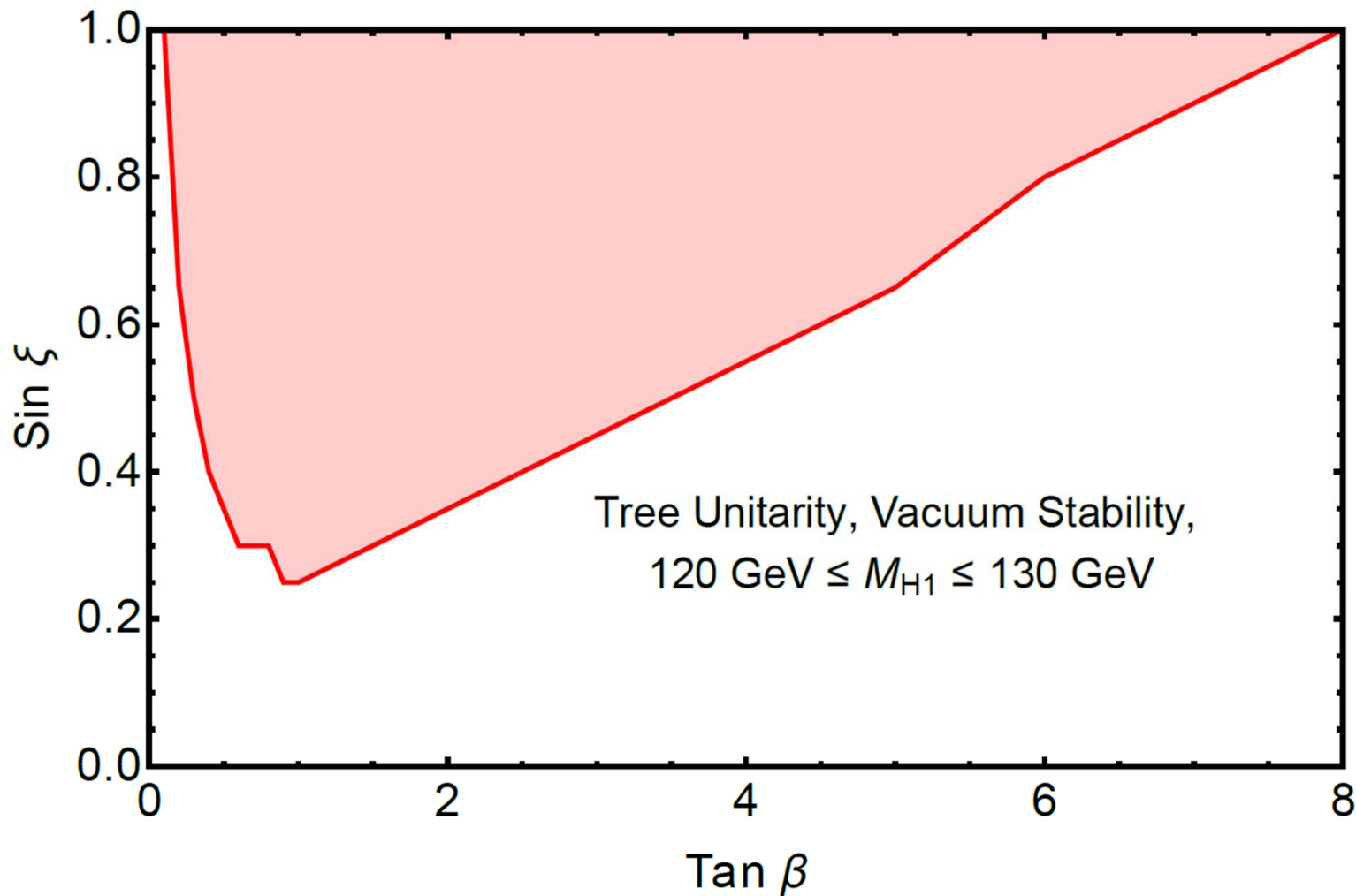
➡ Lower limit on $|\sin \xi|$, lower and upper limit on $\tan \beta$.



□ 10 Parameters : $m_{H_1}, m_{H_2}, m_{H_3}, m_{H^\pm}, \underline{a_{23}, a_{13}, a_{12}}, v, \tan \beta, \sin \xi$.

→ $(a, 0, 0)$ in the Higgs alignment limit

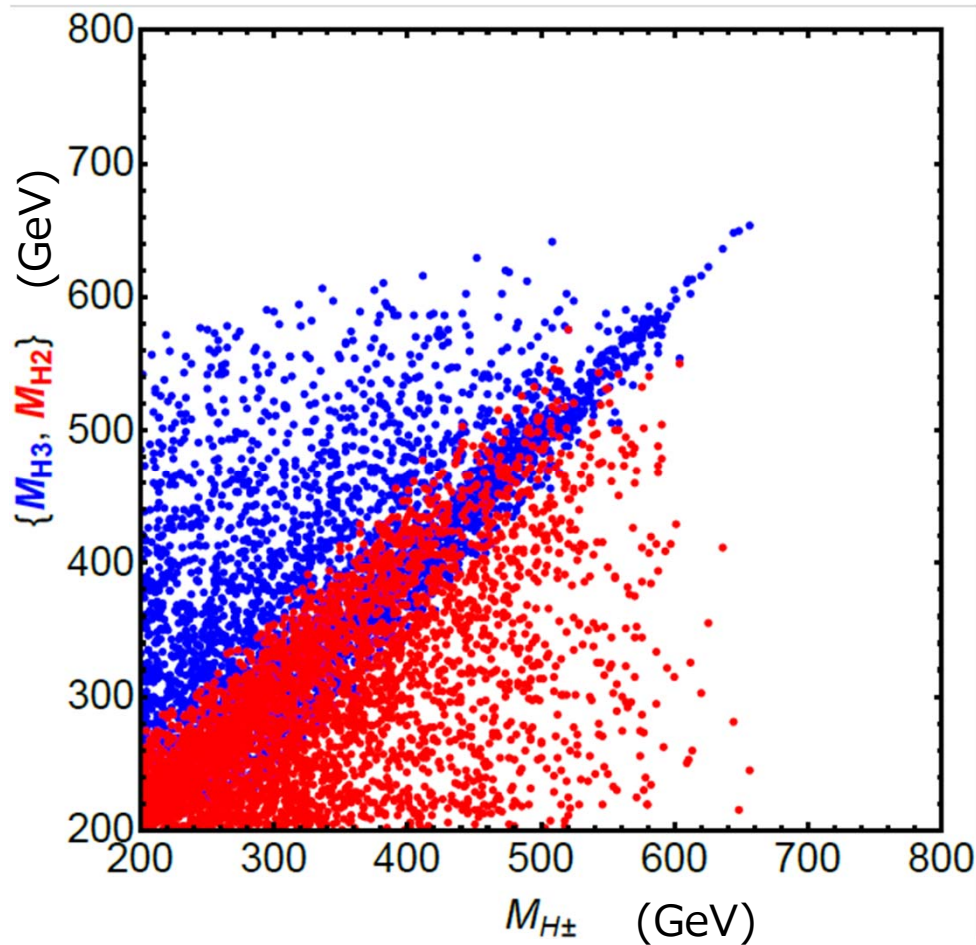
Limit on $\tan\beta$ – $\sin\xi$ plane



$$0.1 \lesssim \tan \beta \lesssim 10, \quad |\sin \xi| \gtrsim 0.3$$

Limit on $m_{H^\pm}$ - $m_{H_{2,3}}$ plane

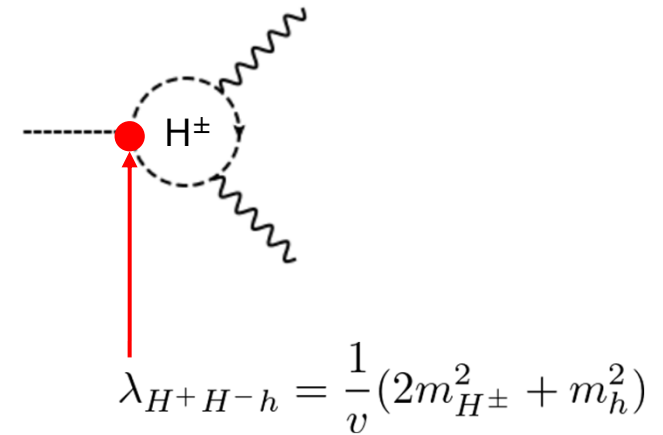
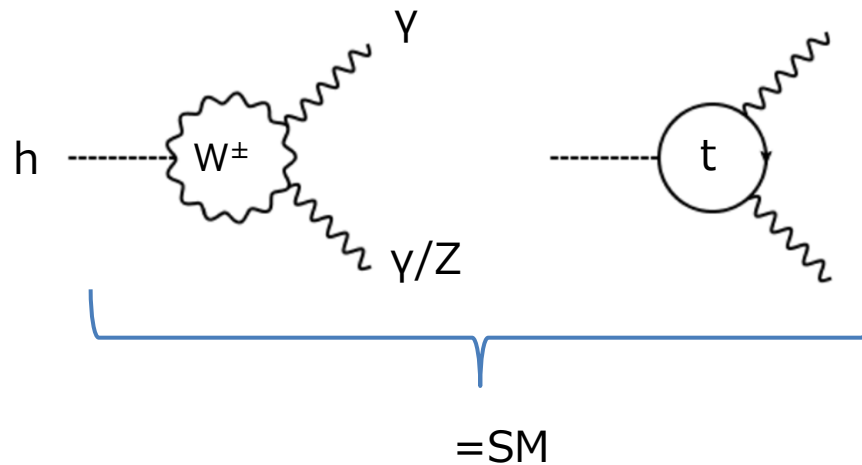
NLO unitarity bound: Nierste, Mustafa, Tabet, Robert, Ziegler (2020)



$$m_{H^\pm} \lesssim 650 \text{ GeV}, \quad m_{H_2} \lesssim 600 \text{ GeV}, \quad m_{H_3} \lesssim 700 \text{ GeV}$$

$h \rightarrow \gamma\gamma/Z\gamma$

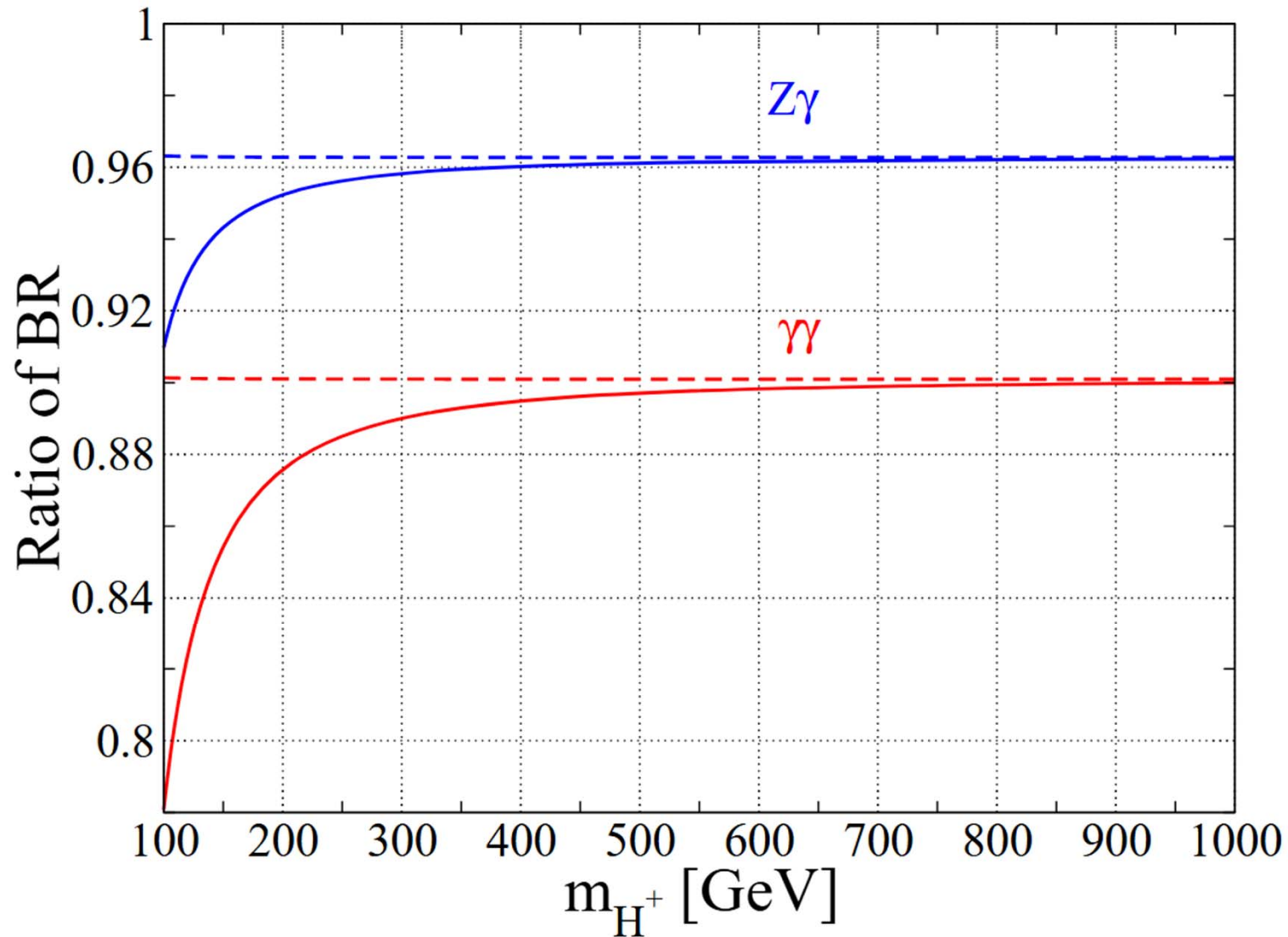
- We take the Higgs alignment limit.



$$\Gamma(h \rightarrow \gamma\gamma) = \frac{\alpha_{\text{em}}^2 m_h^3}{16\pi^3 v^2} \left| \underbrace{(W, t\text{-loop})}_{\sim 1.6} - \underbrace{\frac{1}{24} \frac{v \lambda_{H^+H^-h}}{m_{H^\pm}^2}}_{\sim 1/12} + \mathcal{O}\left(\frac{m_h^2}{m_{H^\pm}^2}\right) \right|^2$$

$h \rightarrow \gamma\gamma/Z\gamma$

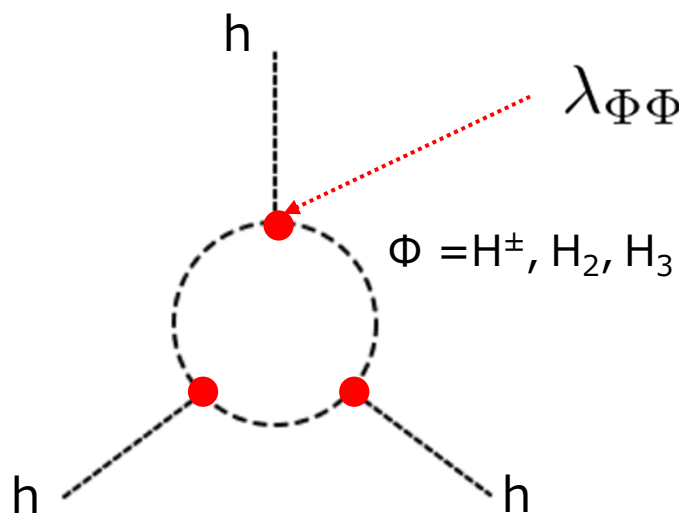
2-loop: Aiko, Braathen, Kanemura (2023)
Degrassi, Slavich (2023)



Self-coupling

1-loop: Kanemura, Okada, Senaha, Yuan (2004)

2-loop: Braathen, Kanemura (2019)



$$\lambda_{\Phi\Phi h} = \frac{1}{v}(2m_\Phi^2 + m_h^2)$$

$$\lambda_{ABC} \equiv \frac{\partial^3 V}{\partial A \partial B \partial C}$$

$$\simeq \frac{1}{32\pi^2} \left(\frac{2\lambda_{H^+H^-h}^3}{m_{H^\pm}^2} + \frac{\lambda_{H_2H_2h}^3}{m_{H_2}^2} + \frac{\lambda_{H_3H_3h}^3}{m_{H_3}^2} \right)$$

$$\simeq \frac{1}{32\pi^2 v^3} (2m_{H^\pm}^4 + m_{H_2}^4 + m_{H_3}^4)$$

cf. 2HDM w/o SCPV

$$\frac{1}{32\pi^2 v^3} \left[2m_{H^\pm}^4 \left(1 - \frac{M^2}{m_{H^\pm}^2} \right)^3 + m_{H_2}^4 \left(1 - \frac{M^2}{m_{H_2}^2} \right)^3 + m_{H_3}^4 \left(1 - \frac{M^2}{m_{H_3}^2} \right)^3 \right]$$

The SCPV 2HDM **predicts** the maximal non-decoupling loop effect.

Yukawa interactions

- Up-type quark sector (down sectors are similar)

$$\begin{aligned}\mathcal{L}_Y &= -\bar{Q}_L \left(Y_1 \tilde{\Phi}_1 + Y_2 \tilde{\Phi}_2 \right) u_R + \text{h.c.} & Y_1, Y_2: \text{Real matrices} \\ &= -\bar{Q}_L \left(\frac{\sqrt{2}}{v} \tilde{M}_u \tilde{\Phi} + \tilde{\rho}_u \tilde{\Phi}' \right) u_R + \text{h.c.}\end{aligned}$$

$$\text{where } \tilde{M}_u = \frac{v}{\sqrt{2}} (Y_1 \cos \beta + e^{-i\xi} Y_2 \sin \beta), \quad \tilde{\rho}_u = -Y_1 \sin \beta + e^{-i\xi} Y_2 \cos \beta$$

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- Biunitary transformation makes the mass matrix diagonal:

$$u_L \rightarrow V_u u_L, \quad u_R \rightarrow U_u u_R$$

$$\tilde{M}_u \rightarrow M_u = V_u^\dagger \tilde{M}_u U_u \quad (\text{diagonal}) \quad \tilde{\rho}_u \rightarrow \rho_u = V_u^\dagger \tilde{\rho}_u U_u$$

- Reality condition, $\text{Im}[Y_1] = \text{Im}[Y_2] = 0$, restricts the structure of ρ_u matrix.

$$\rho_u = \frac{1}{\sqrt{2} c_\beta s_\beta v} \left[\left(c_{2\beta} + \frac{i}{t_\xi} \right) M_u - \left(1 + \frac{i}{t_\xi} \right) (V_u^\dagger V_u^* M_u U_u^T U_u) \right]$$

Yukawa alignment

▣ If we impose the **Yukawa alignment** condition $Y_2 = \zeta_u Y_1$ ($\zeta_u \in \mathbb{R}$)

$$\tilde{M}_u = \frac{v}{\sqrt{2}} Y_1 (\cos \beta + \underbrace{e^{-i\xi} \zeta_u \sin \beta}_{\text{complex parameter}}), \quad \tilde{\rho}_u = Y_1 (\underbrace{-\sin \beta + e^{-i\xi} \zeta_u \cos \beta}_{\text{complex parameter}})$$

- We can diagonalize two matrices at the same time. 😊
- Complex phase can be removed by quark rephasing. 😞
→ KM phase vanishes. So, we need **Yukawa misalignment**.

Yukawa alignment

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- We can diagonalize two matrices at the same time. 
- Complex phase can be removed by quark rephasing. 
- KM phase vanishes. So, we need **Yukawa misalignment**

- ▣ We **partially** impose the Yukawa alignment for d/e sectors.

$$\rho_{d/e} = \frac{\sqrt{2} M_{d/e}}{v} \left(\frac{-t_\beta + \zeta_{d/e} e^{i\xi}}{1 + \zeta_{d/e} t_\beta e^{i\xi}} \right)$$

$$V_{\text{CKM}} = V_u^\dagger V_d$$

$$\rho_u = \frac{1}{\sqrt{2} c_\beta s_\beta v} \left[\left(c_{2\beta} + \frac{i}{t_\xi} \right) M_u - \left(1 + \frac{i}{t_\xi} \right) (V_{\text{CKM}} V_{\text{CKM}}^T M_u U_u^T U_u) \right]$$

Constraints on ρ_u

□ Now, flavor violating interaction comes from ρ_u .

$$\rho_u = \frac{1}{\sqrt{2}c_\beta s_\beta v} \left[\left(c_{2\beta} + \frac{i}{t_\xi} \right) M_u - \left(1 + \frac{i}{t_\xi} \right) \underbrace{(V_{\text{CKM}} V_{\text{CKM}}^T M_u U_u^T U_u)}_{\sim \mathbf{I} + \epsilon (10^{-3}-10^{-4})} \right]$$

• Ex 1: U_u to be orthogonal with a phase factor

$$\rho_u = \frac{\sqrt{2}M_u}{v} \zeta_u + \mathcal{O}(\epsilon) \quad \zeta_u = \frac{1}{s_{2\beta}} \left[c_{2\beta} + \frac{i}{t_\xi} - \left(1 + \frac{i}{t_\xi} \right) e^{2i\theta_u} \right]$$

→ Yukawa alignment like scenario

• Ex 2: U_u to be (2,3) rotation, i.e.,

$$U_u = \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos \theta & e^{-i\delta} \sin \theta \\ 0 & -e^{i\delta} \sin \theta & \cos \theta \end{pmatrix}$$

$$\rho_u = \frac{1}{\sqrt{2}c_\beta s_\beta v} \left[\left(c_{2\beta} + \frac{i}{t_\xi} \right) M_u - \left(1 + \frac{i}{t_\xi} \right) \underbrace{(V_{\text{CKM}} V_{\text{CKM}}^T M_u U_u^T U_u)}_{\sim \mathbf{I} + \epsilon (10^{-3}-10^{-4})} \right]$$

$$m_t \begin{pmatrix} \mathcal{O}(r_u) & \mathcal{O}(\epsilon) & \mathcal{O}(\epsilon) \\ \mathcal{O}(\epsilon r_u) & \mathcal{O}(r_c) & \mathcal{O}(r_c) \\ \mathcal{O}(\epsilon r_u) & \mathcal{O}(1) & \mathcal{O}(1) \end{pmatrix} \quad r_u = \frac{m_u}{m_t}, \quad r_c = \frac{m_c}{m_t}$$

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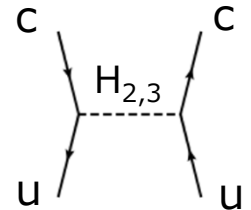
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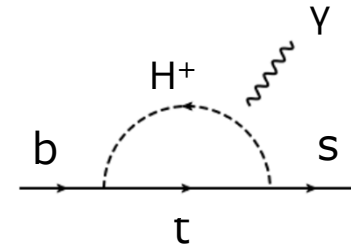
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$$r_u = \frac{m_u}{m_t}, \quad r_c = \frac{m_c}{m_t}$$

Constraints on ρ_u

Now, flavor violating interaction comes from ρ_u .

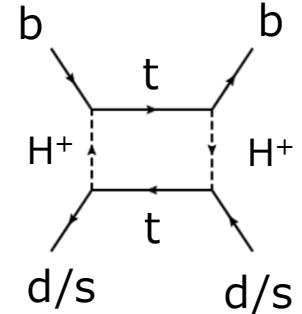
$$\rho_u = \frac{1}{\sqrt{2}c_\beta s_\beta v} \left[\left(c_{2\beta} + \frac{i}{t_\xi} \right) M_u - \left(1 + \frac{i}{t_\xi} \right) \underbrace{(V_{\text{CKM}} V_{\text{CKM}}^T M_u U_u^T U_u)}_{\sim \mathbf{I} + \epsilon (10^{-3}-10^{-4})} \right]$$



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• Ex 2: U_u to be (2,3) rotation, i.e.,

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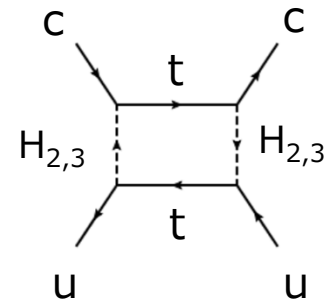
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• Ex 2: U_u to be (2,3) rotation, i.e.,

$$U_u = \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos \theta & e^{-i\delta} \sin \theta \\ 0 & -e^{i\delta} \sin \theta & \cos \theta \end{pmatrix}$$



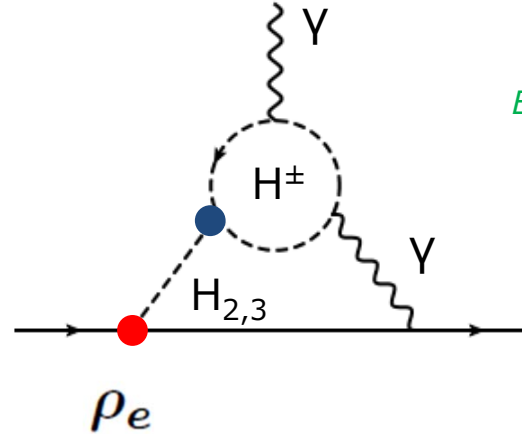
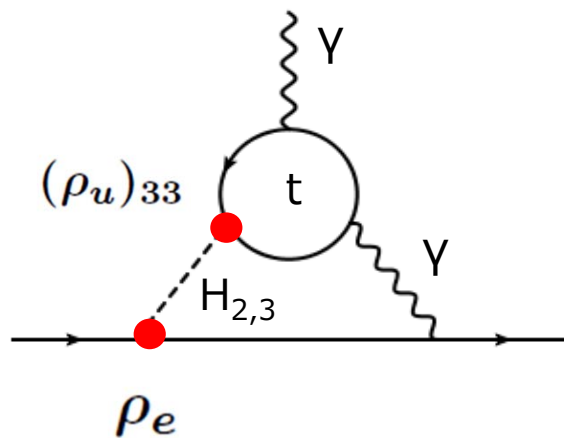
$$\rho_u = \frac{1}{\sqrt{2}c_\beta s_\beta v} \left[\left(c_{2\beta} + \frac{i}{t_\xi} \right) M_u - \left(1 + \frac{i}{t_\xi} \right) \underbrace{(V_{\text{CKM}} V_{\text{CKM}}^T M_u U_u^T U_u)}_{\sim \mathbf{I} + \epsilon (10^{-3}-10^{-4})} \right] \quad |(\rho_u)_{31}(\rho_u)_{32}| < \mathcal{O}(10^{-2})$$

$$m_t \begin{pmatrix} \mathcal{O}(r_u) & \mathcal{O}(\epsilon) & \mathcal{O}(\epsilon) \\ \mathcal{O}(\epsilon r_u) & \mathcal{O}(r_c) & \mathcal{O}(r_c) \\ \mathcal{O}(\epsilon r_u) & \mathcal{O}(1) & \mathcal{O}(1) \end{pmatrix}$$

$$r_u = \frac{m_u}{m_t}, \quad r_c = \frac{m_c}{m_t}$$

EDM Constraints

- Barr-Zee diagrams give dominant contribution to the electron EDM.



Barr, Zee (1990)

$$d_e \sim \left(\frac{1}{16\pi} \right)^2 \times e^3 G_F m_e \sim 10^{-27} \text{ e cm}$$

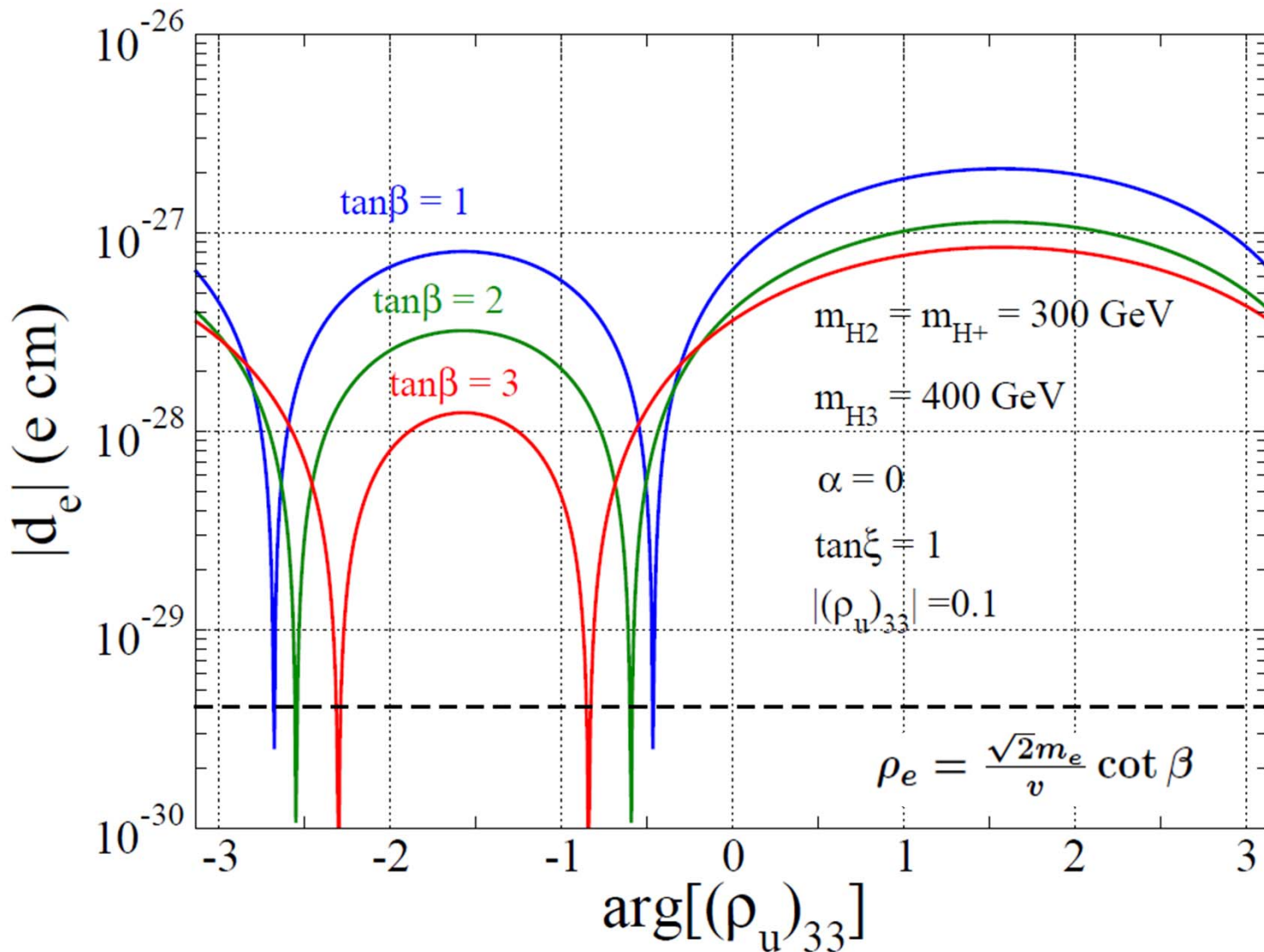
$$\lambda_{H^+H^-H_2} = -\frac{m_{H_2}^2}{vs_\beta c_\beta} (c_\alpha c_{2\beta} + s_\alpha \cot \xi),$$

$$\lambda_{H^+H^-H_3} = -\frac{m_{H_3}^2}{vs_\beta c_\beta} (c_\alpha \cot \xi - s_\alpha c_{2\beta}),$$

$$|d_e| \leq 4.1 \times 10^{-30} \text{ e cm} \quad @ 90\% \text{ CL}$$

Roussy, et.al, arXiv: 2212.11841

EDM Constraints



Correlation b/w $\Delta\kappa_h$ and $h \rightarrow \gamma\gamma$

$$\Delta\kappa_\lambda = \frac{\Delta\lambda_{hhh}^{1\text{-loop}}}{(\lambda_{hhh}^{1\text{-loop}})_{\text{SM}}}$$

Current Limit : $-1.4 \leq \Delta\kappa_\lambda \leq 5.3$

Projected : $\Delta\kappa_\lambda < 1.3$

$$\Delta\mathcal{B}_{h \rightarrow \gamma\gamma} = \frac{\mathcal{B}_{h \rightarrow \gamma\gamma}^{2\text{HDM}}}{\mathcal{B}_{h \rightarrow \gamma\gamma}^{\text{SM}}} - 1,$$

ATLAS : $-0.12 \leq \Delta\mathcal{B}_{h \rightarrow \gamma\gamma} \leq 0.18$

Projected : $\Delta\mathcal{B}_{h \rightarrow \gamma\gamma} @ 4\%$

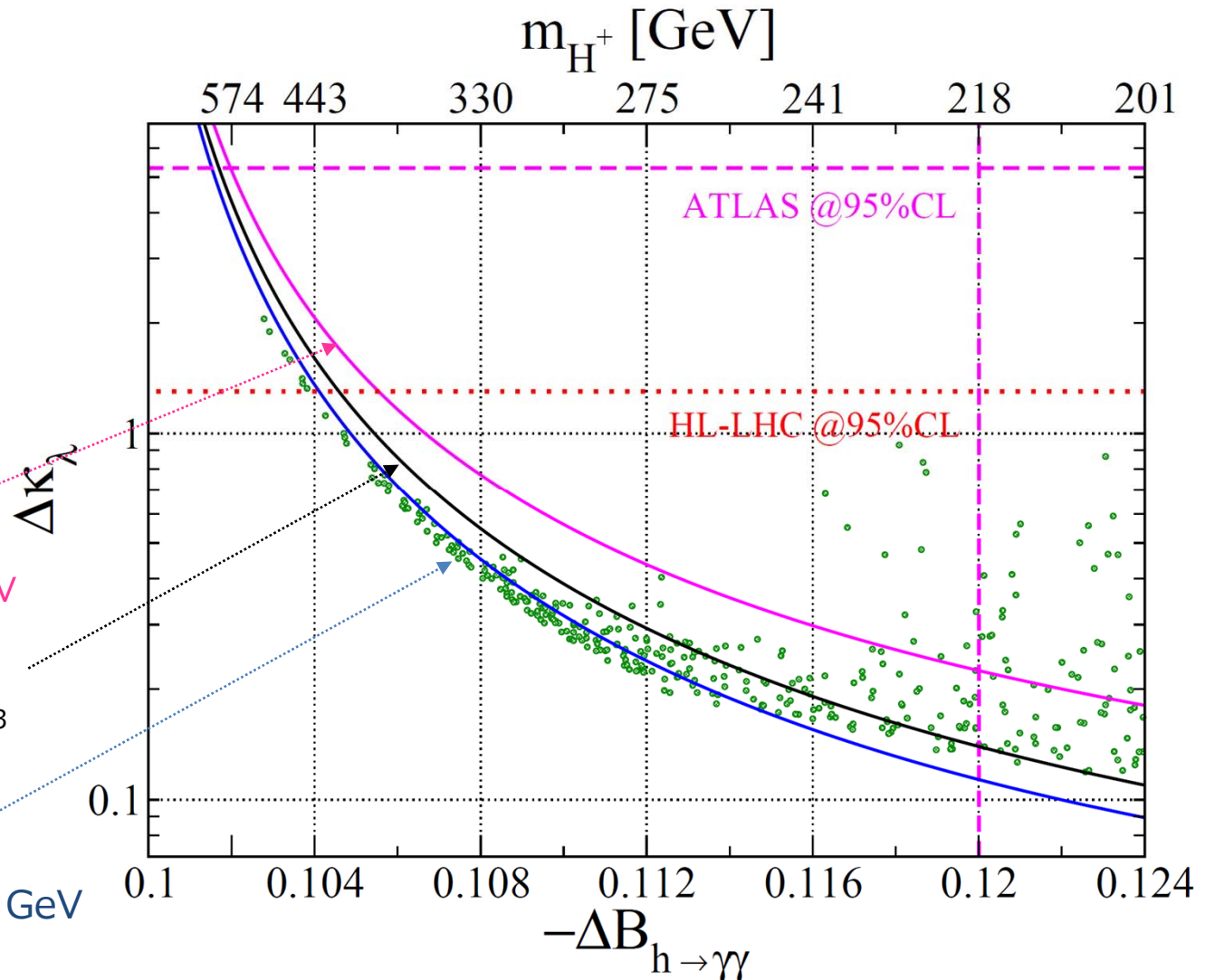
$m_{H^+} = m_{H_3},$

$m_{H_3} - m_{H_2} = 100 \text{ GeV}$

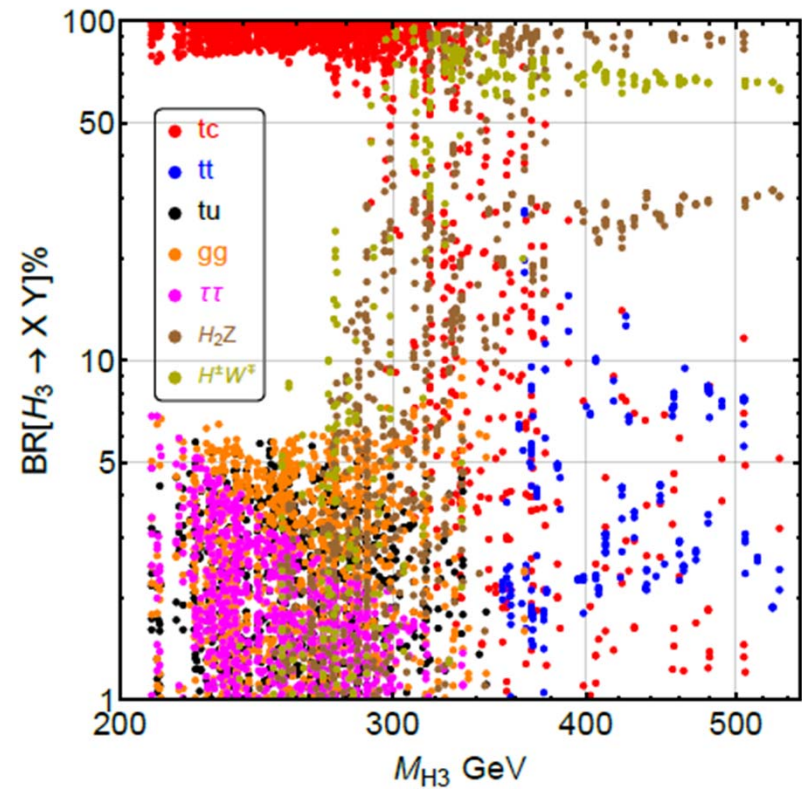
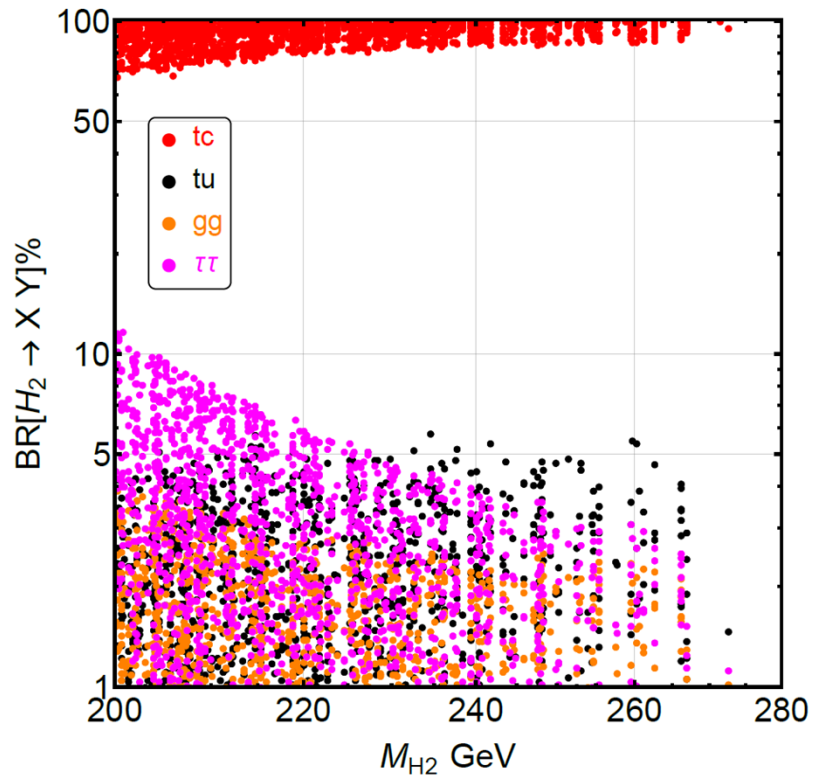
$m_{H^+} = m_{H_2} = m_{H_3}$

$m_{H^+} = m_{H_2},$

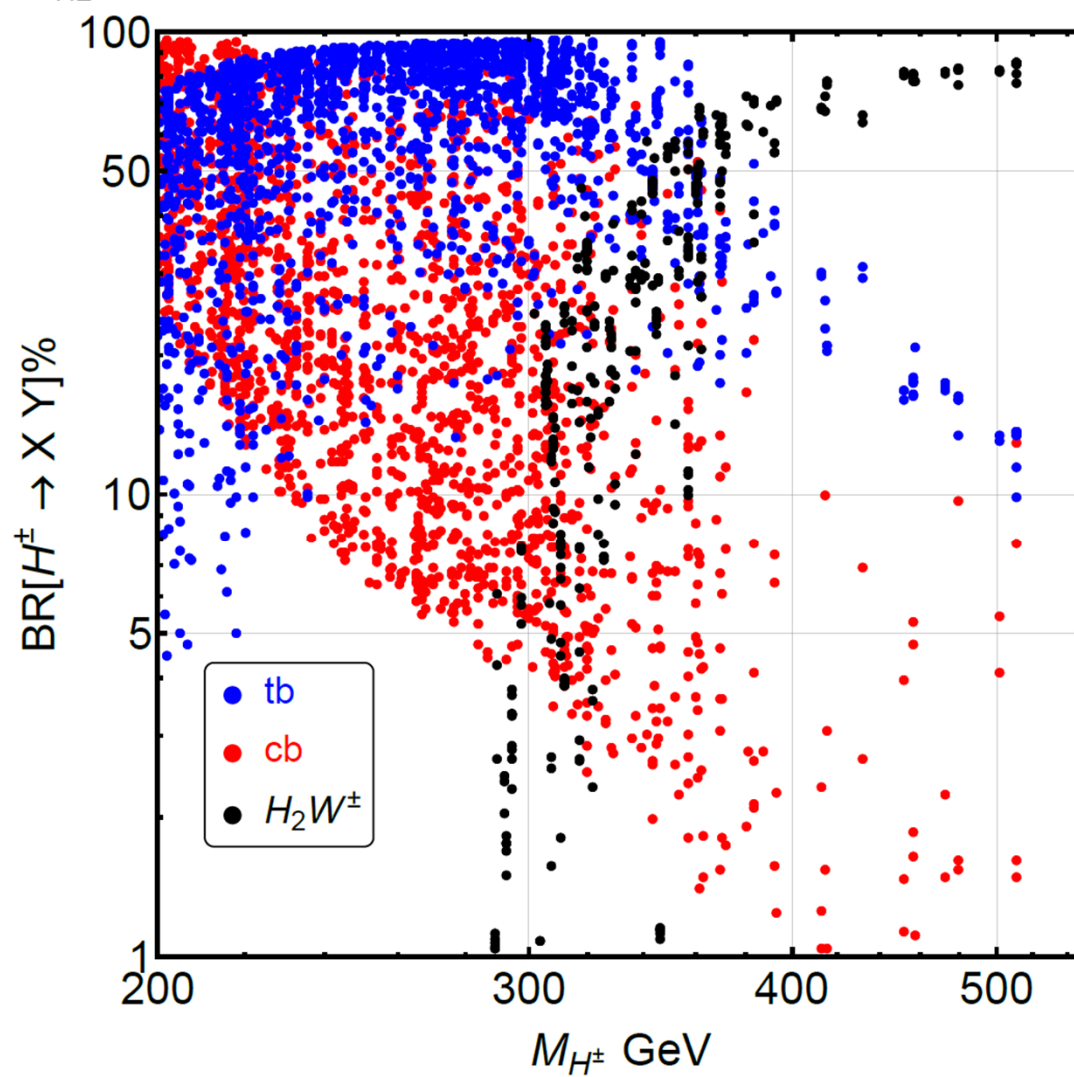
$m_{H_3} - m_{H_2} = 100 \text{ GeV}$



Decay BR of H_2 and H_3



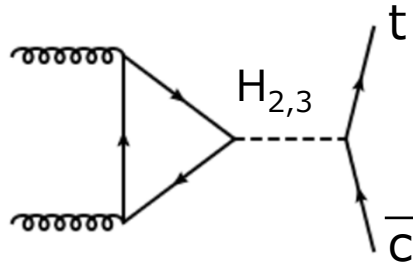
Decay BR of $H^\pm$



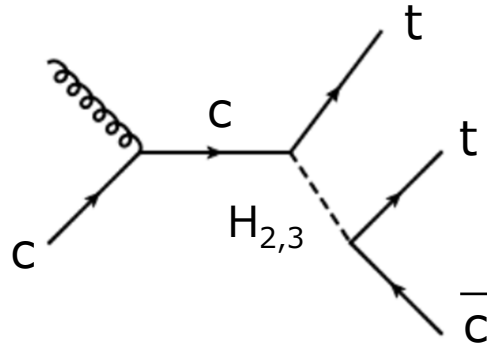
Collider signatures (on going)

- Characteristic signatures via multi-top events appear from $[\rho_u]_{32}$

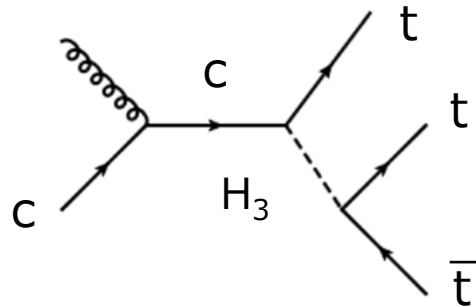
- Mono-top



- Di-top

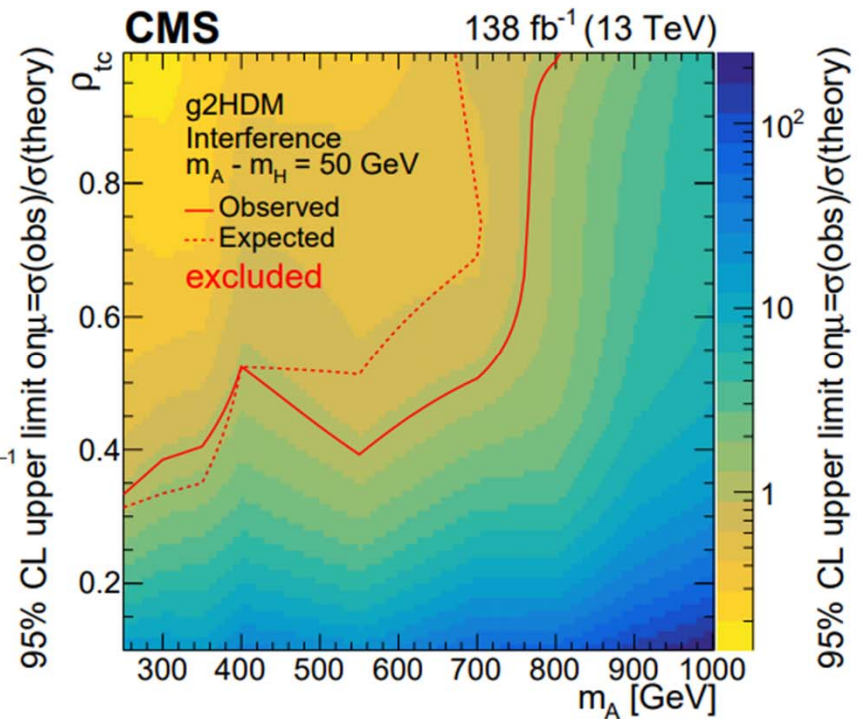
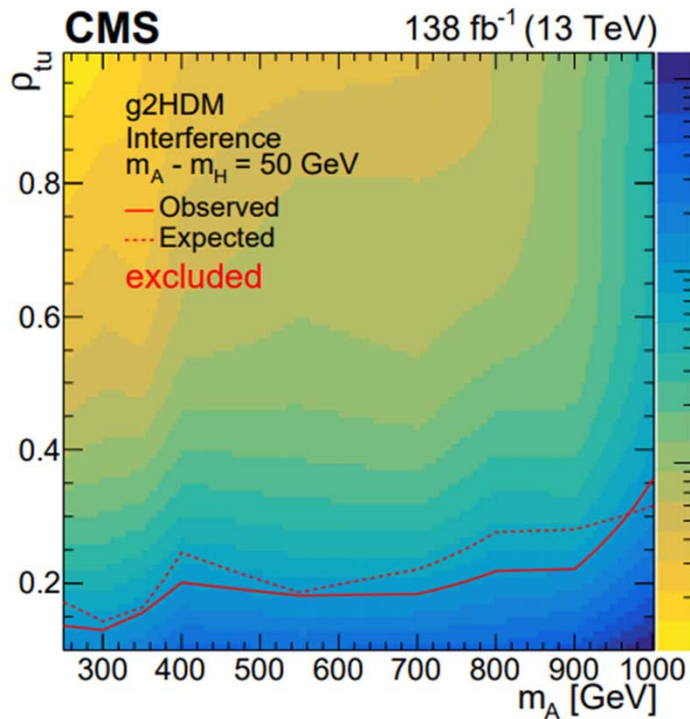
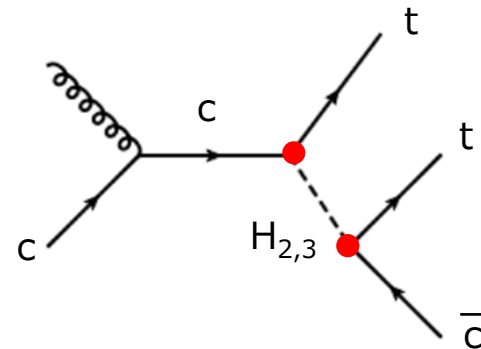
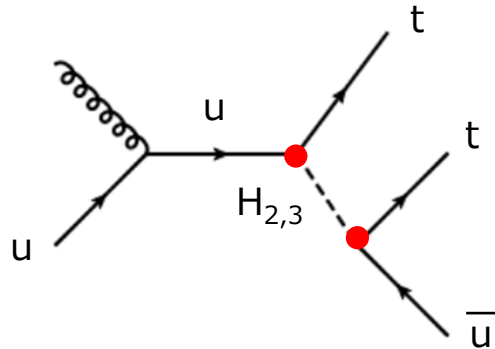


- Triple-top



Smoking gun: Top number violating signatures w/ charm

Current bounds on ρ_{31} and ρ_{32}



Summary

SCPV 2HDM

Inevitable non-decoupling Higgs sectors

Flavor misalignment

