

# Biases in Mass Estimate of Galaxy Clusters

mainly on X-ray observations

## 銀河団の質量測定バイアス

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# Introduction

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- Mass of galaxy clusters
  - cosmological parameters (through mass function)

- Impact on cosmological parameters

- $\sigma_8$  from cluster abundance (Shimizu et al., 2006)

$$\sigma_{8,\text{true}} = \sigma_{8,\text{cluster}} + 0.5(1 - \alpha_M) \quad \alpha_M = M_{\text{est}}/M_{\text{tot}} @r_{\text{vir}}$$

- discrepancy between CMB & cluster abundance

- Ongoing & future projects

- ASTRO-H, eROSITA (X-ray)
- Planck, SPT, ACT (Sunyaev-Zel'dovich effect)
- Subaru HSC (Lensing)

→ Large sample of clusters

Accurate mass measurement becomes more important!

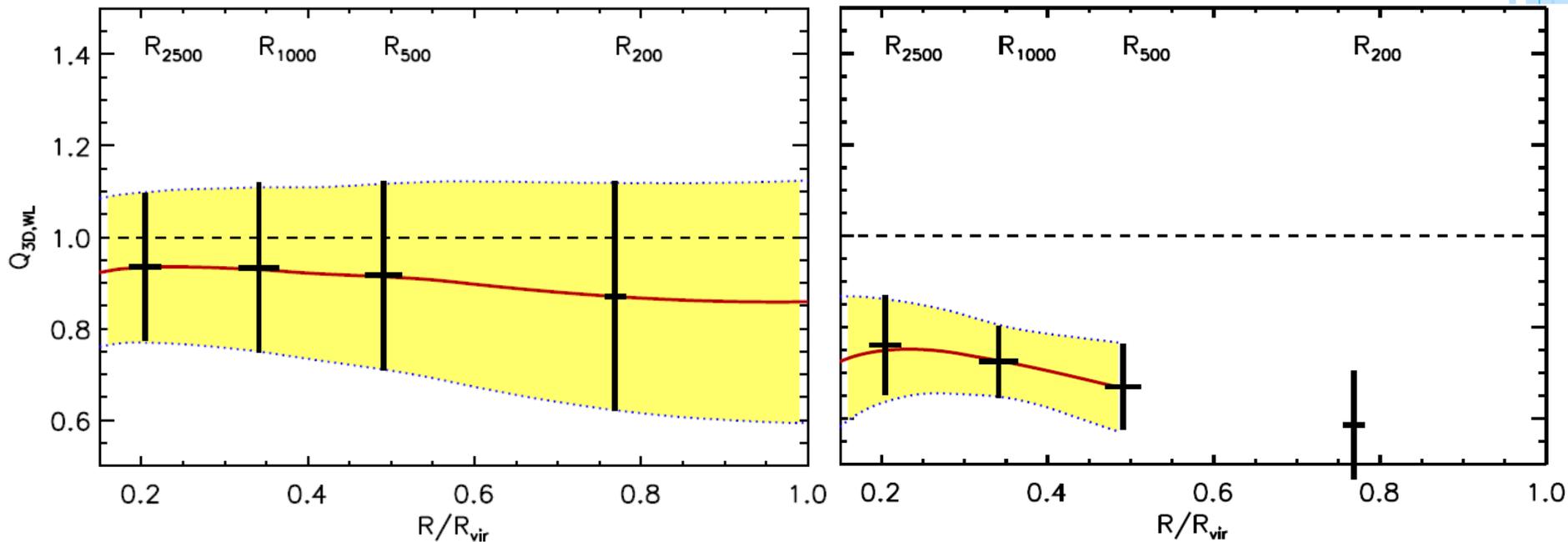


# Mock Observations

- Mock observations (Rasia et al., 2012)
  - 20 clusters  $\times$  3 directions
  - weak lensing (assuming HST) : more accurate, larger scatter
  - X-ray (assuming Chandra) : less accurate, smaller scatter

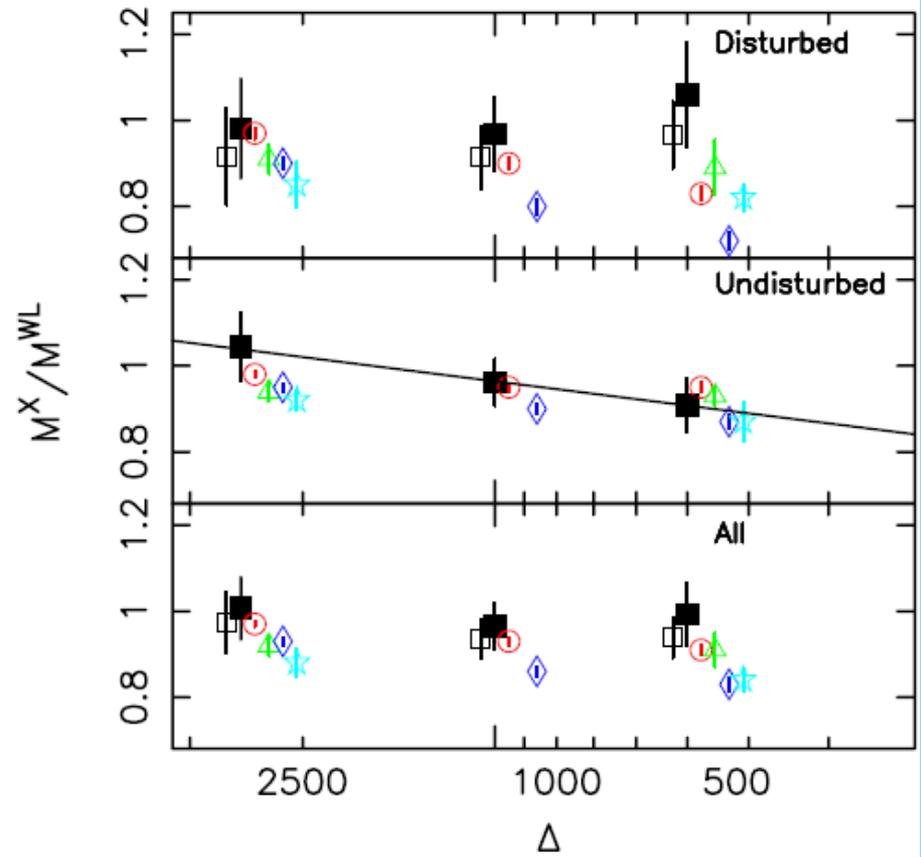
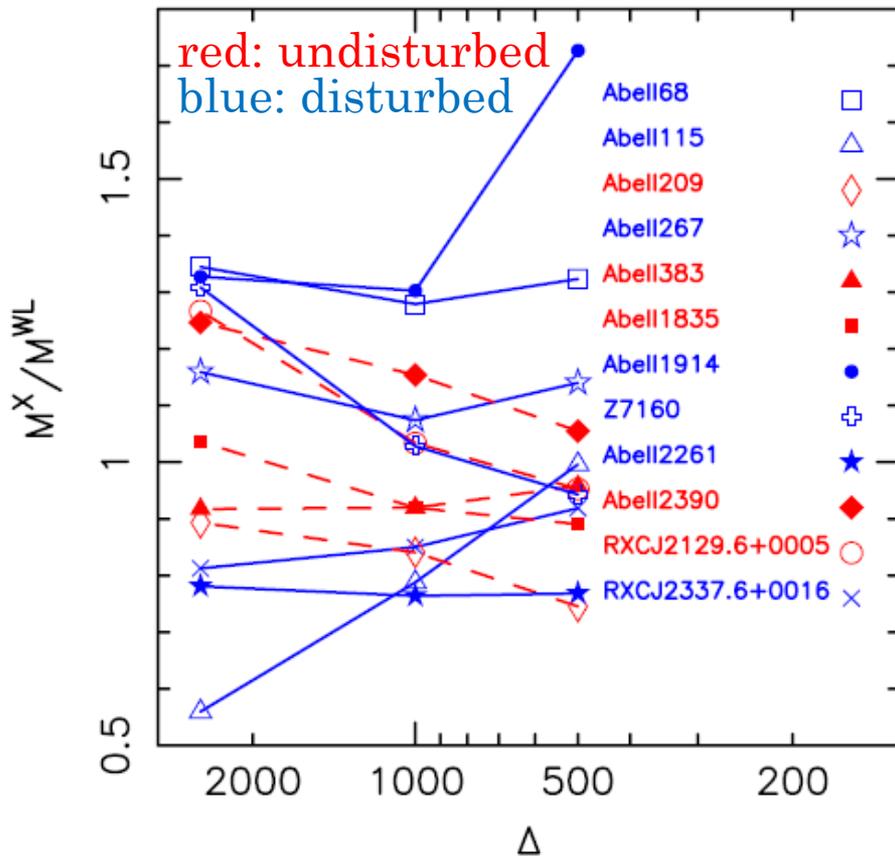
↓  $M_{\text{obs}}/M_{\text{true}}$  WL

X



# X-ray vs. Weak Lensing

- 12 clusters observed in WL (Subaru) & X-ray (XMM-Newton) (Zhang et al., 2010)



# Causes of the Bias

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- Gravitational Lensing

- substructure
- non-sphericity
- ...

- X-ray & Sunyaev-Zel'dovich effect

- assumption of hydrostatic equilibrium (HSE)
- deprojection of gas properties from 2D observables  
(related to non-sphericity)
- ...



# Hydrostatic Equilibrium (X-ray)

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- Observables

- surface brightness & spectroscopic (projected) temperature  
→ gas density  $n(r)$  & (deprojected) temperature  $T(r)$

- Hydrostatic Equilibrium (HSE)

$$-\frac{1}{\rho_{\text{gas}}} \frac{dp}{dr} = \frac{GM}{r^2}$$

$$M_{\text{HSE}} = -\frac{k_B T(r)}{\mu m_p G} \left[ \frac{d \log n(r)}{d \log r} + \frac{d \log T(r)}{d \log r} \right]$$

The accuracy of X-ray mass estimate depends on the validity of HSE assumption



# Hydrostatic Equilibrium (SZ)

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- Observable

$Y \sim$  l.o.s. integral of gas pressure

1. combined with gas density or temperature from X-ray  
→ estimate mass under the HSE assumption

OR

2. Y-M scaling relation constructed by combining M-T relation with other scaling relations  
→ scaling relations are calibrated by X-ray observations & simulations

Mass estimate of SZ effect is also based on HSE assumption.



# Equation of Motion of Gas

↓ Gravitational Potential

$$\nabla\Phi = -\frac{1}{\rho_{\text{gas}}}\nabla p - \frac{\partial\mathbf{v}}{\partial t} - (\mathbf{v}\cdot\nabla)\mathbf{v}$$

HSE

Euler Eq. (simulations)

+ (terms neglected in simulations)

$$\Delta\Phi = 4\pi G\rho_{\text{tot}}$$

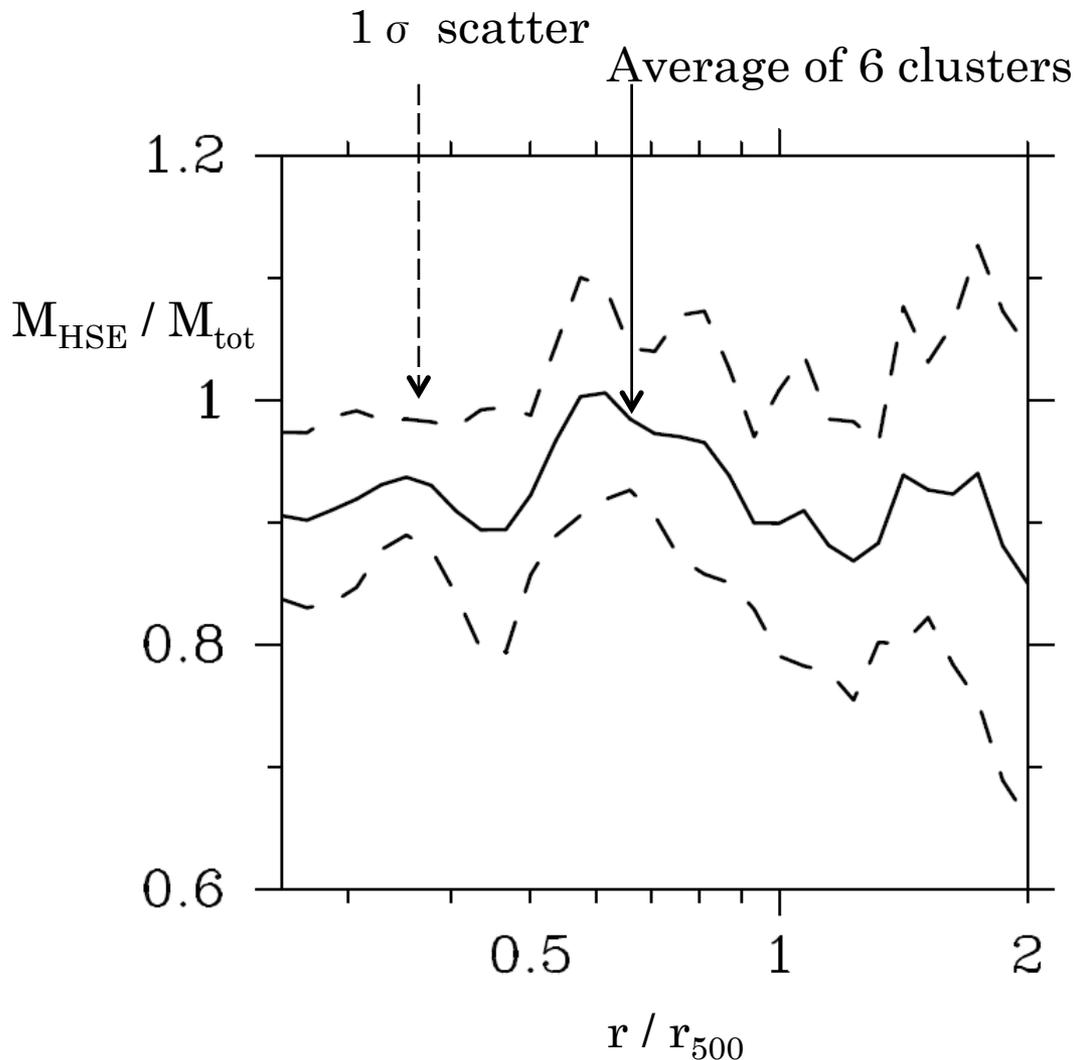
$$-\frac{1}{4\pi G}\int d\mathbf{S}\cdot\frac{\nabla p}{\rho_{\text{gas}}} = M_{\text{HSE}}$$

$$\int d^3x \rho_{\text{tot}} = M_{\text{tot}}$$



# HSE Mass vs. Total Mass

- 1 AMR & 5 SPH simulated clusters (DS+13)  
(relaxed)



HSE Mass / Total Mass is  
 $\sim 0.9 @ r_{500}$   
& can be  $>30\%$  @ larger radii

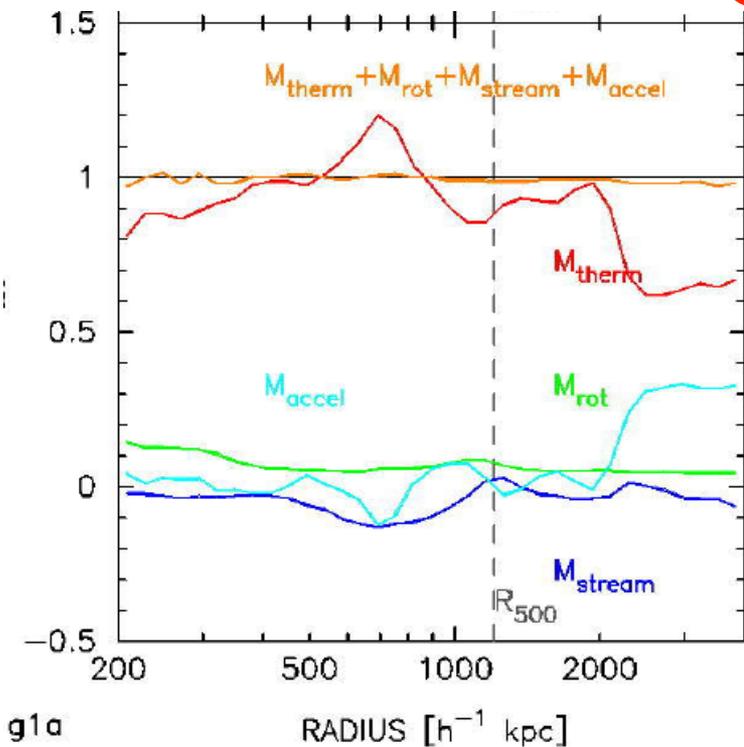
consistent with other studies

- Fang et al., 2009  
(16 clusters)
- Lau et al., 2009  
(16 clusters)
- Lau et al., 2013  
(5 clusters)
- Nelson et al., 2013  
(62 clusters)

# Contribution from Other Terms (1)

$$\nabla\Phi = -\frac{1}{\rho_{\text{gas}}}\nabla p - \frac{\partial\mathbf{v}}{\partial t} - (\mathbf{v}\cdot\nabla)\mathbf{v}$$

$$\int d^3x \rho_{\text{tot}} = \frac{1}{4\pi G} \int dS \left[ \frac{1}{\rho_{\text{gas}}} \frac{\partial p}{\partial r} + \frac{v_{\theta}^2 + v_{\phi}^2}{r} - (\mathbf{v}\cdot\nabla)v_r - \frac{\partial v_r}{\partial t} \right]$$



Acceleration is the most important  
(DS+13, 1 AMR & 5 SPH clusters)

Rotation is the most important  
(Fang et al, 2009;  
same analysis but different sample)

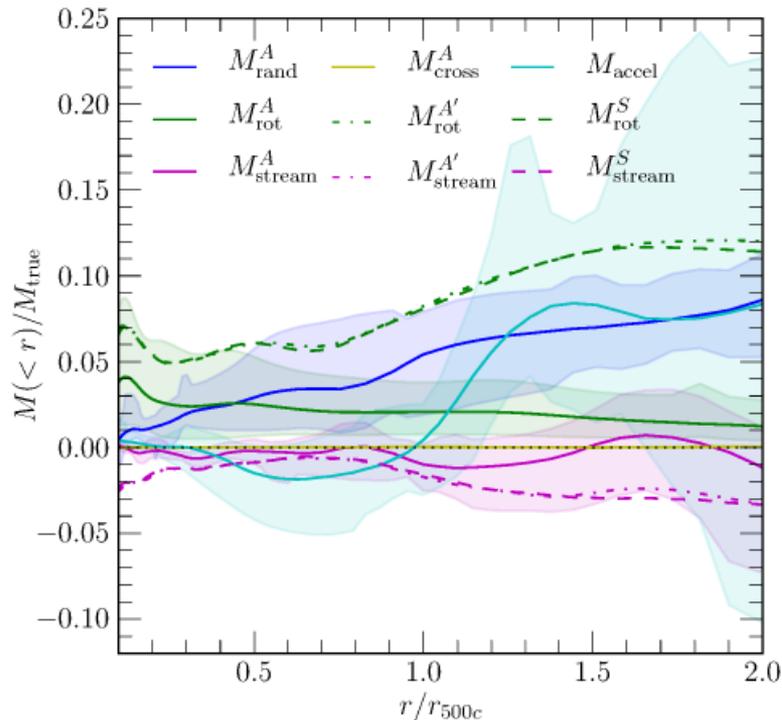


# Contribution from Other Terms (2)

$$\nabla\Phi = -\frac{1}{\rho_{\text{gas}}}\nabla p - \frac{\partial\mathbf{v}}{\partial t} - (\mathbf{v}\cdot\nabla)\mathbf{v} \quad \langle \dots \rangle : \text{mass average}$$

$$M(<r) = \frac{-r^2}{G\langle\rho\rangle} \frac{\partial\langle P\rangle}{\partial r} + \frac{-r^2}{G\langle\rho\rangle} \frac{\partial\langle\rho\rangle\sigma_{\rho,rr}^2}{\partial r} - \frac{r}{G} (2\sigma_{\rho,rr}^2 - \sigma_{\rho,\theta\theta}^2 - \sigma_{\rho,\phi\phi}^2) + \frac{-r^2}{G} \frac{\partial\langle u_r\rangle_\rho}{\partial t} + \frac{r}{G} (\langle u_\theta\rangle_\rho^2 + \langle u_\phi\rangle_\rho^2) - \frac{r^2}{G} \left( \langle u_r\rangle_\rho \frac{\partial\langle u_r\rangle_\rho}{\partial r} + \frac{\langle u_\theta\rangle_\rho}{r} \frac{\partial\langle u_r\rangle_\rho}{\partial\theta} + \frac{\langle u_\phi\rangle_\rho}{r\sin\theta} \frac{\partial\langle u_r\rangle_\rho}{\partial\phi} \right)$$

$$\frac{-r^2}{G\langle\rho\rangle} \left( \frac{1}{r} \frac{\partial\langle\rho\rangle\sigma_{\rho,r\theta}^2}{\partial\theta} + \frac{1}{r\sin\theta} \frac{\partial\langle\rho\rangle\sigma_{\rho,r\phi}^2}{\partial\phi} \right) - \frac{r}{G} (\sigma_{\rho,r\theta}^2 \cot\theta)$$



← average of 5 relaxed clusters (Lau et al., 2013)

Random motion & acceleration have large contribution at large radii

Nelson et al., (2013)

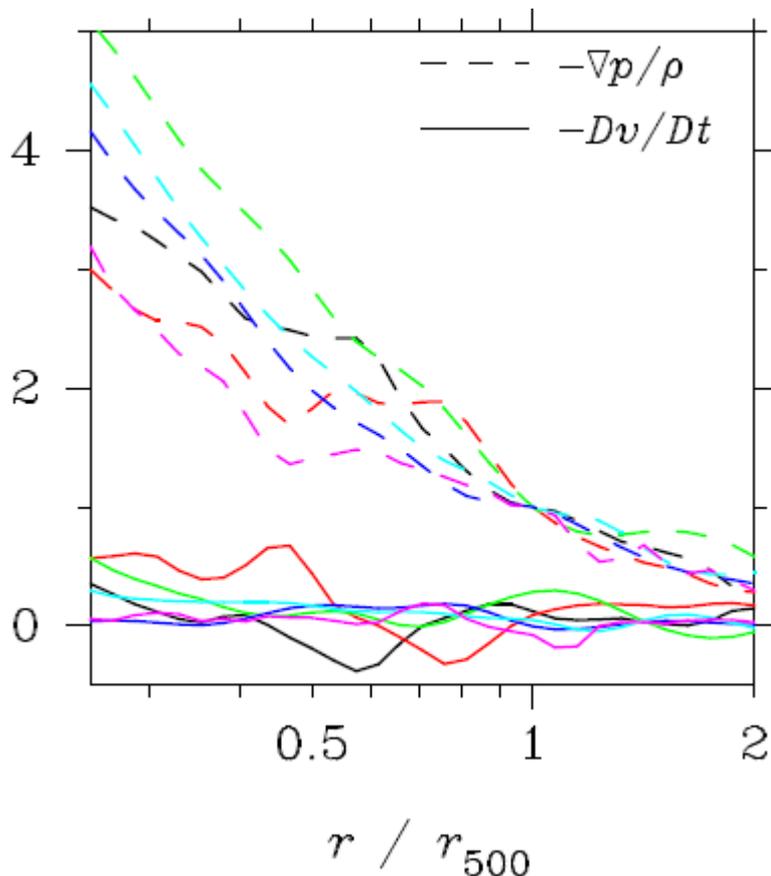
Acceleration has small contribution (<3%) on average (12 relaxed clusters), but it produces a large scatter



# Contribution from Other Terms (3)

$$\nabla\Phi = -\frac{1}{\rho_{\text{gas}}}\nabla p - \frac{\partial\mathbf{v}}{\partial t} - (\mathbf{v}\cdot\nabla)\mathbf{v} = -\frac{D\mathbf{v}}{Dt} \quad (\text{Lagrangian acceleration})$$

normalized by  $|\nabla p/\rho(r_{500})|$



- $Dv/Dt$  is roughly constant compared to  $\nabla p/\rho$
- Surface integral converges them to mass terms
- **The contribution of  $Dv/Dt$  becomes more larger at larger radii**
- velocity: will be observed with ASTRO-H (dynamical picture of clusters!)
- acceleration
- things neglected in simulations (e.g. non-thermal pressure from cosmic rays etc.)



# Causes of the Bias

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- Gravitational Lensing

- substructure
- non-sphericity
- ...

- X-ray & Sunyaev-Zel'dovich effect

- assumption of hydrostatic equilibrium (HSE)
  - ~10% @  $r_{500}$ , >30% @ larger radii

- deprojection of gas properties from 2D observables  
(related to non-sphericity of clusters)

- ...



# Deprojection Effect (1)

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- Surface brightness  $I_X$  & spectroscopic temperature  $T_{\text{spec}}$   
→ Radial profiles of density  $n(r)$  & temperature  $T(r)$   
deprojection process can produce another bias

DS+(in prep)

$$T_{\text{sl}} = \frac{\int dl n^2 T^{1/4}}{\int dl n^2 T^{-3/4}}$$

- make  $I_X$  & spectroscopic-like temperature  $T_{\text{sl}}$  from simulation data (1 AMR and 5 SPH clusters)
- find  $n(r)$  &  $T(r)$  which best reproduce  $I_X$  &  $T_{\text{sl}}$  assuming

$$\hat{n}(r) = n_0 \frac{(r/r_c)^{-\alpha/2}}{(1 + r^2/r_c^2)^{3\beta/2 - \alpha/4}} \quad \hat{T}(r) = T_0 \frac{(r/r_t)^{-a}}{(1 + (r/r_t)^b)^{c/b}}$$

Vikhlinin et al., 2006

- calculate HSE mass

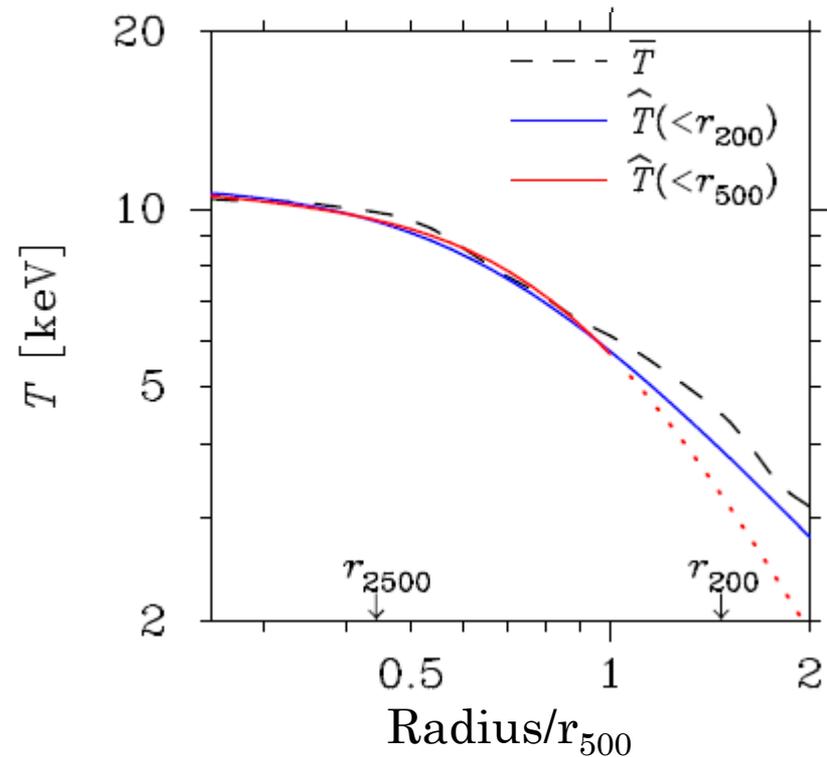
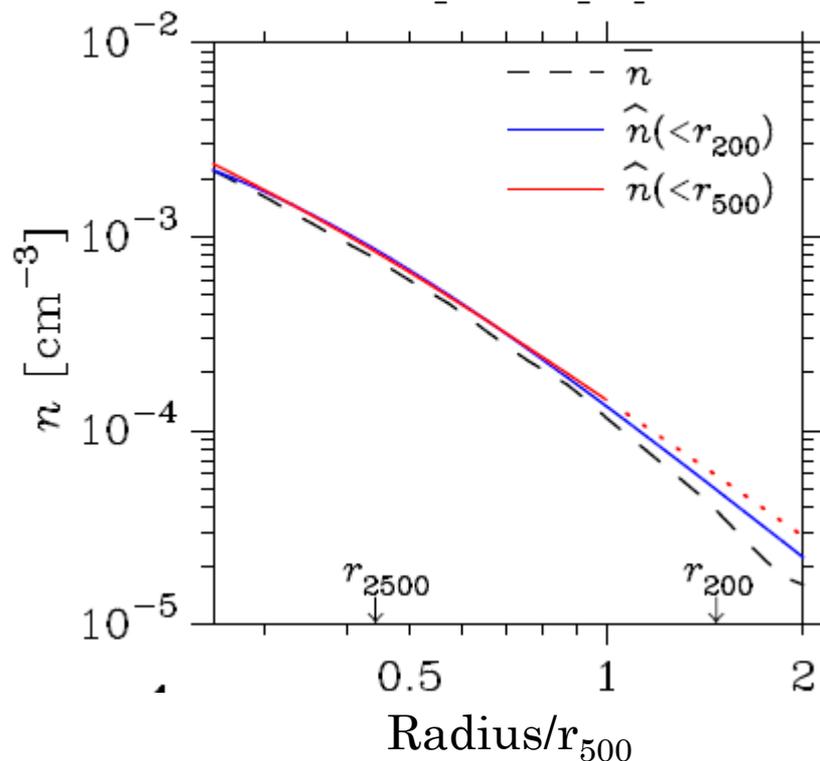
$$M_{\text{HSE}} = -\frac{k_B T(r)}{\mu m_p G} \left[ \frac{d \log n(r)}{d \log r} + \frac{d \log T(r)}{d \log r} \right]$$



# Deprojection Effect (2)

- # of bins: arbitrary
- error bars: variance in the annulus

NOT considering some specific observation



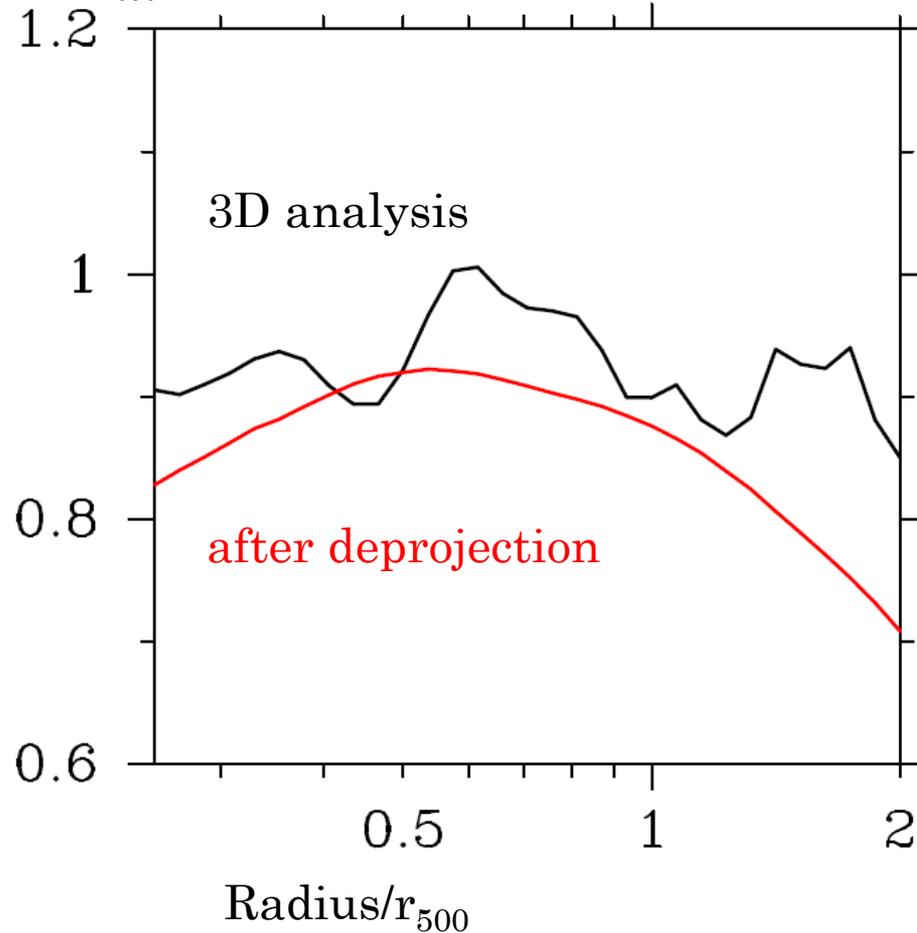
Density: tend to be overestimated (observables  $\propto n^2$ )  
Temperature: tend to be underestimated



# Deprojection Effect (3)

$$M_{\text{HSE}} = -\frac{k_B T(r)}{\mu m_p G} \left[ \frac{d \log n(r)}{d \log r} + \frac{d \log T(r)}{d \log r} \right]$$

$M_{\text{HSE}} / M_{\text{tot}}$  (average of 6 clusters)



Deprojection yields another  
~10% underestimate of mass



# Causes of the Bias

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## ○ Gravitational Lensing

- substructure
- non-sphericity
- ...

## ○ X-ray & Sunyaev-Zel'dovich effect

- assumption of hydrostatic equilibrium (HSE)
  - underestimate by  $\sim 10\%$  @  $r_{500}$ ,  $>30\%$  @ larger radii
- deprojection of gas properties from 2D observables  
(related to non-sphericity of clusters)
  - another  $\sim 10\%$  underestimate
- ...



# Discussion

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- assumption of hydrostatic equilibrium (HSE)
  - underestimate by  $\sim 10\%$  @  $r_{500}$ ,  $>30\%$  @ larger radii
- deprojection of gas properties from 2D observables (related to non-sphericity of clusters)
  - another  $\sim 10\%$  underestimate

- consistent with Rasia et al. (2012)

( $\sim 20\%$  @  $r_{500}$  underestimate with large scatter)

larger radii?? things neglected in simulations??

treatment of high energy physics in simulations?

- To better estimate mass...

1. accurately measure gas density & temperature

e.g. using variance in  $I_x$  to correct the bias in density ( $\sqrt{n^2} \rightarrow n$ )

(Roncarelli et al., 2013)

2. reconcile the discrepancy between HSE mass & total mass

# Summary

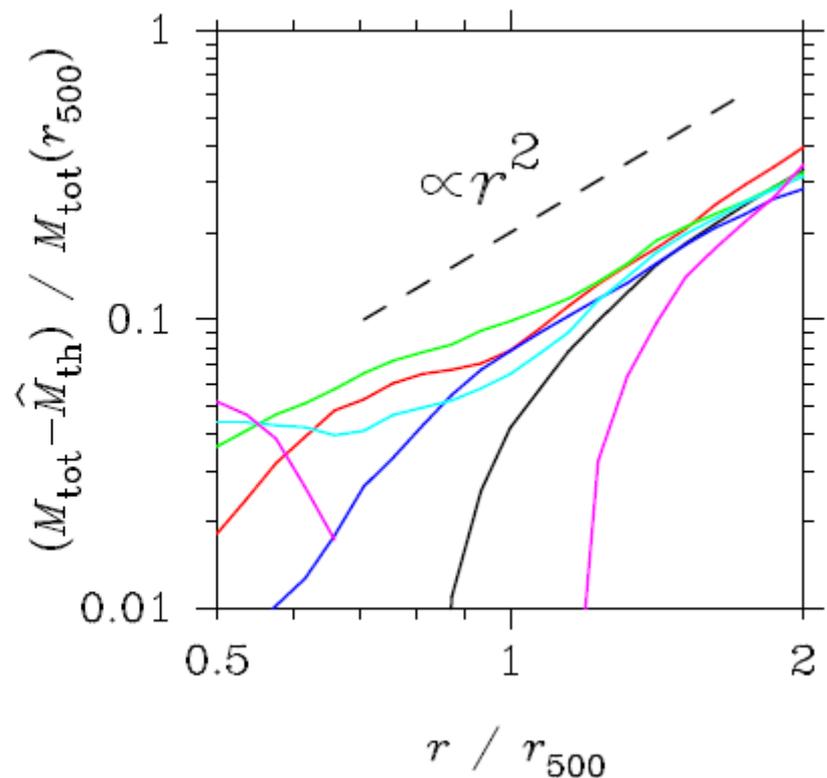
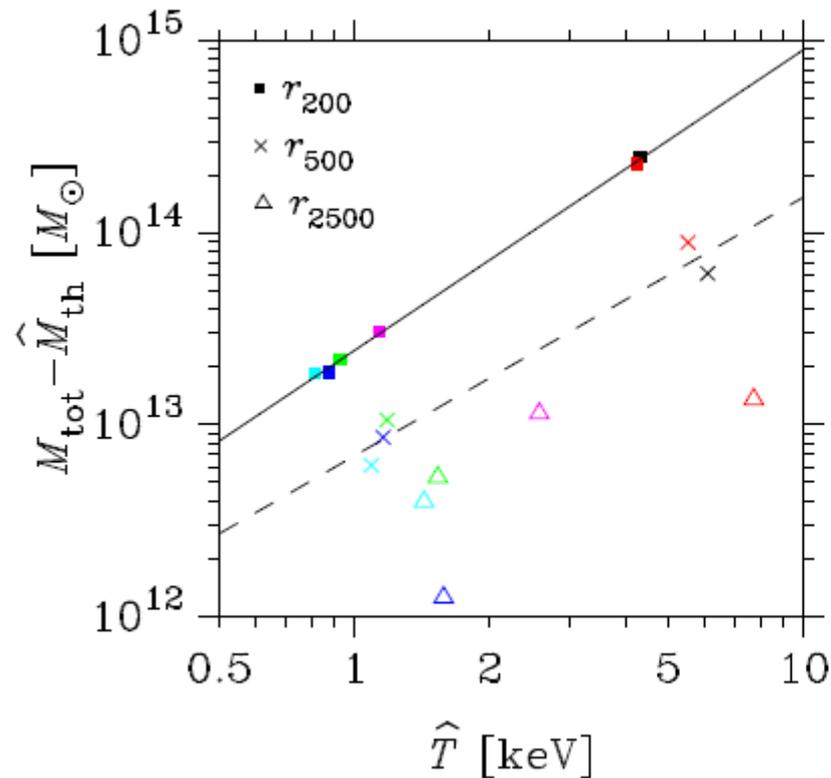
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- According to Rasia et al. (2012)
  - Lensing mass underestimates the true mass by <10% on average with large scatter
  - X-ray hydrostatic mass underestimates the true mass by >20% on average with small scatter
- Bias in X-ray observations
  - assumption of hydrostatic equilibrium (HSE)
    - underestimate by ~10% @  $r_{500}$ , >30% @ larger radii
  - deprojection of gas properties from 2D observables (related to non-sphericity of clusters)
    - another ~10% underestimate
  - Effect neglected in simulations can be significant in real clusters



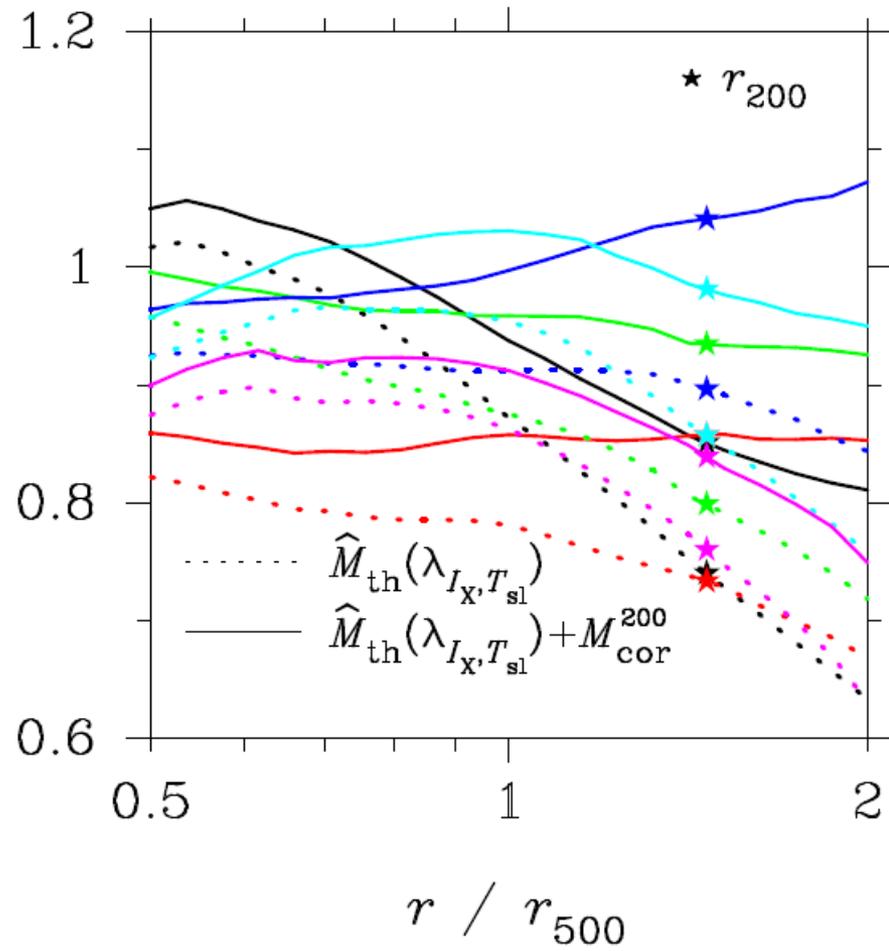
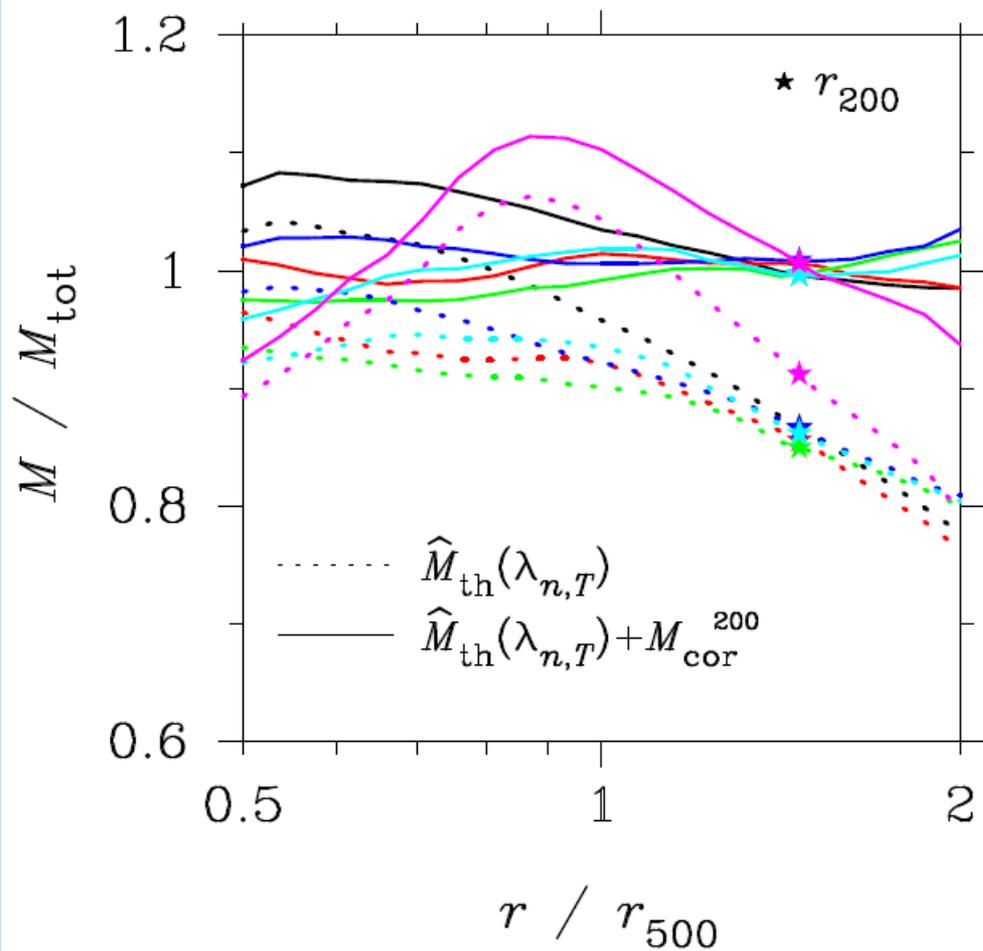
# Correction Term

$$M_{\text{cor}}^{\Delta} = A_{\Delta} \left( \frac{T(r_{\Delta})}{\text{keV}} \right)^{B_{\Delta}} \left( \frac{r}{r_{\Delta}} \right)^{C_{\Delta}} M_{\odot}$$



$$M_{\text{cor}}^{200} = \left( \frac{\hat{T}(r_{200})}{\text{keV}} \right)^{1.75} \left( \frac{r}{r_{200}} \right)^2 \times 10^{13.4} M_{\odot} \quad M_{\text{cor}}^{500} = \left( \frac{\hat{T}(r_{500})}{\text{keV}} \right)^{1.35} \left( \frac{r}{r_{500}} \right)^2 \times 10^{12.8} M_{\odot}$$

# Correction Term



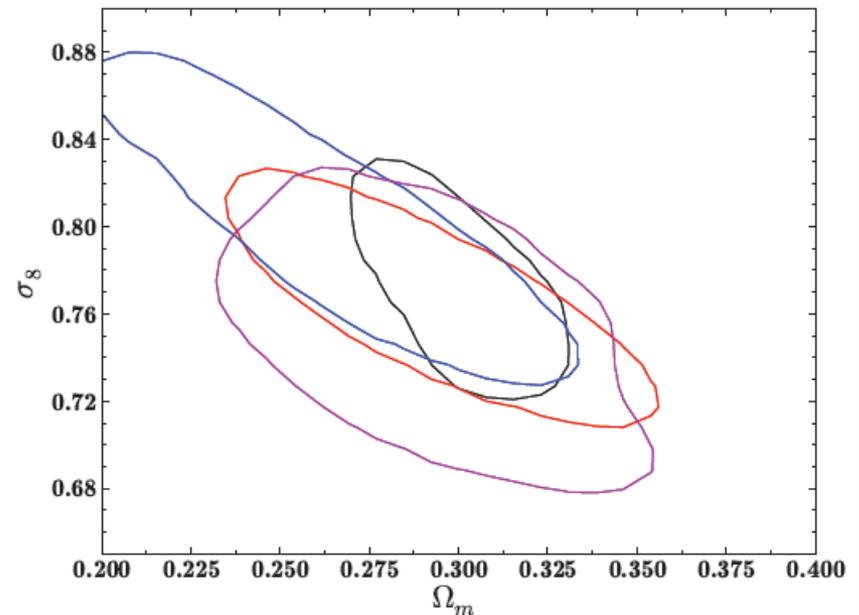
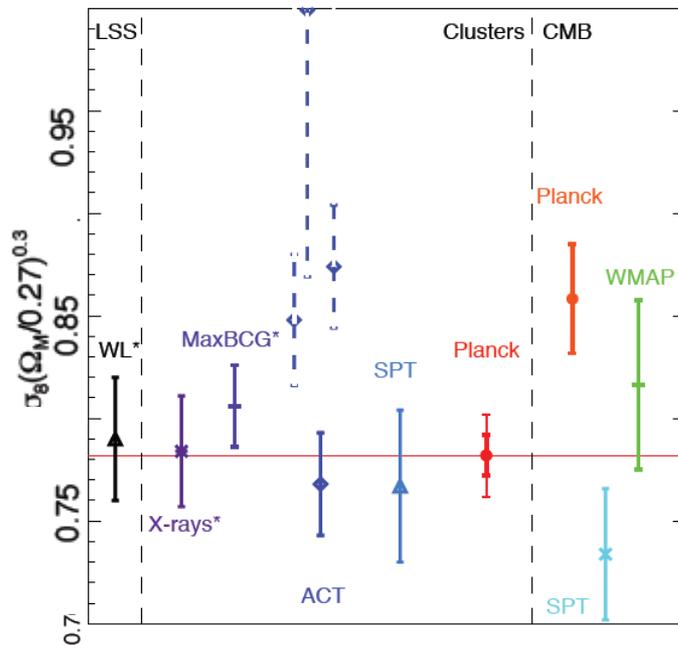
# Introduction

- Impact on cosmological parameters

- $\sigma_8$  from cluster abundance (Shimizu et al., 2006)

$$\sigma_{8,\text{true}} = \sigma_{8,\text{cluster}} + 0.5(1 - \alpha_M) \quad \alpha_M = M_{\text{est}}/M_{\text{tot}}$$

- Cluster abundance vs. CMB anisotropies



# Entropy

